

# DANGO

## Danish National Galileo Overlay

### Final Presentation

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Image credit: [https://www.esa.int/ESA\\_Multimedia/Images/2015/09/Denmark\\_from\\_the\\_ISS](https://www.esa.int/ESA_Multimedia/Images/2015/09/Denmark_from_the_ISS)

# Introduction - Danish National Galileo Overlay

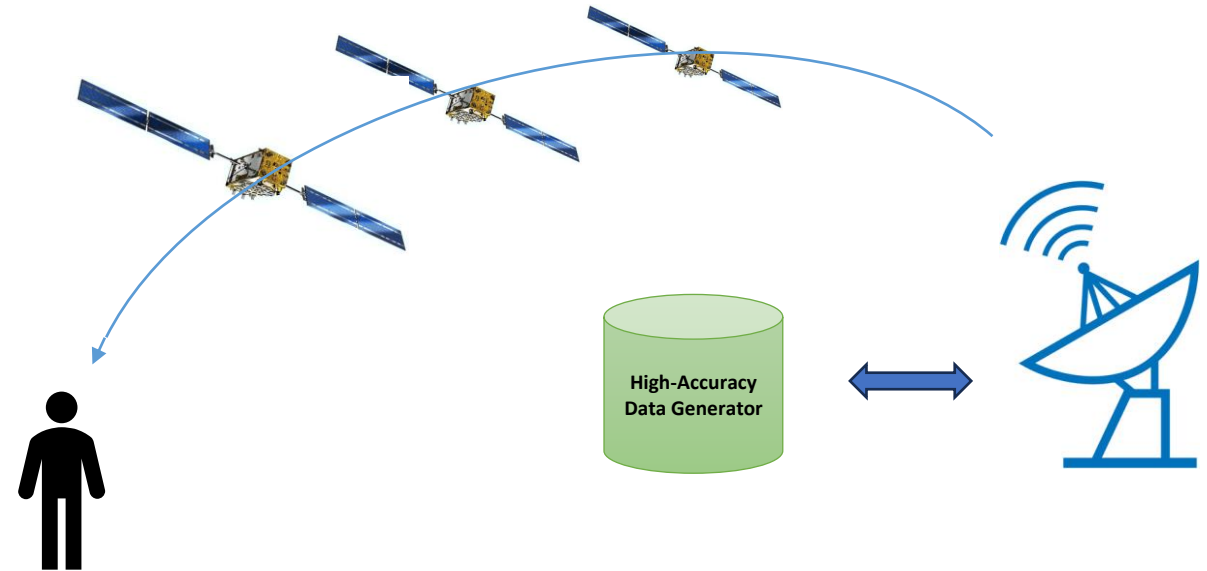
# The Galileo Overlay

- Galileo High Accuracy Service (Galileo HAS)
- Novel PPP service
- Interest to utilize the Galileo HAS in Denmark

**The challenge:** HAS PPP corrections come in Galileo Terrestrial Reference System (GTRS).

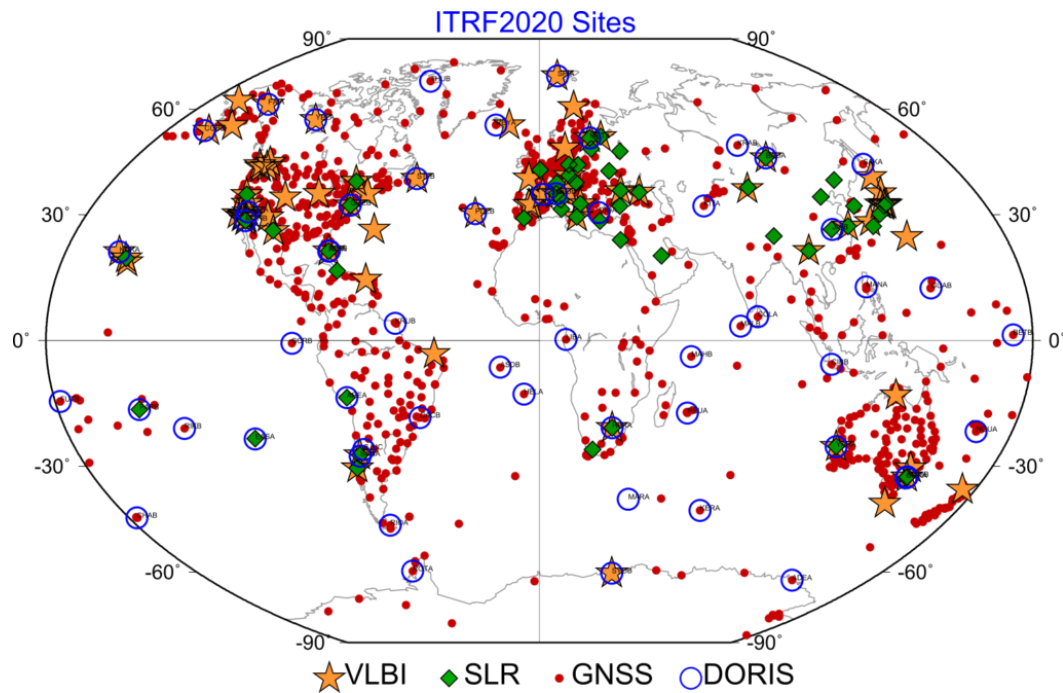
GTRS is equivalent to International Terrestrial Reference System (ITRS).

**GTRS = ITRS**

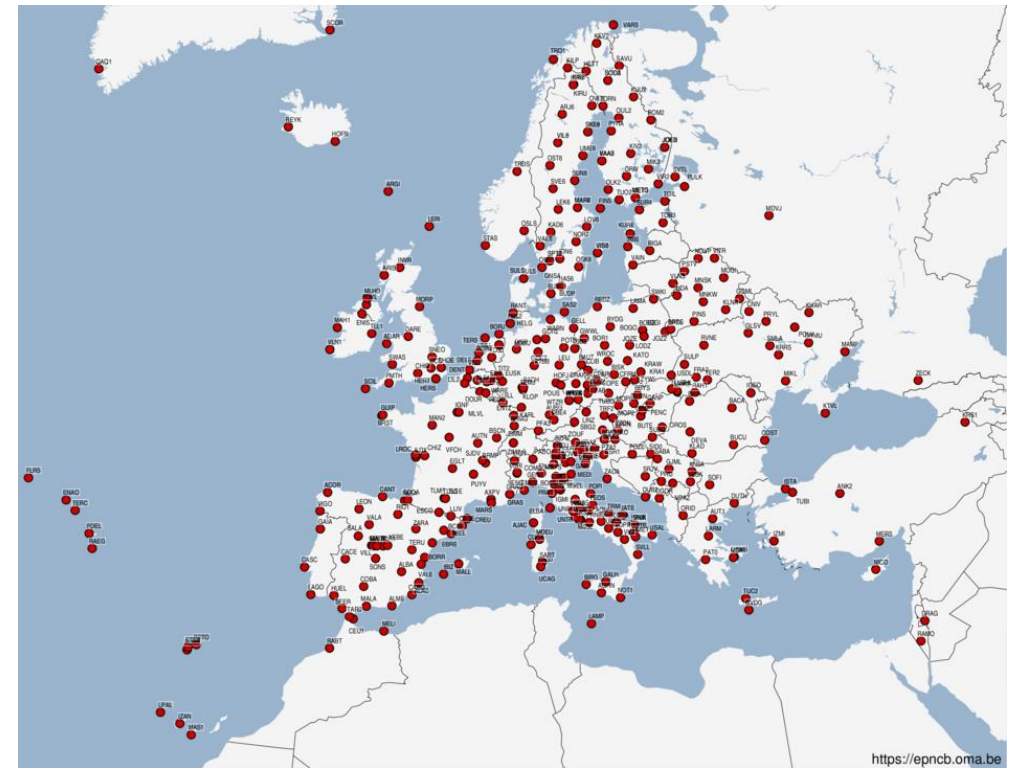


# Reference frame transformations

ITRS  $\approx$  ETRS89DK

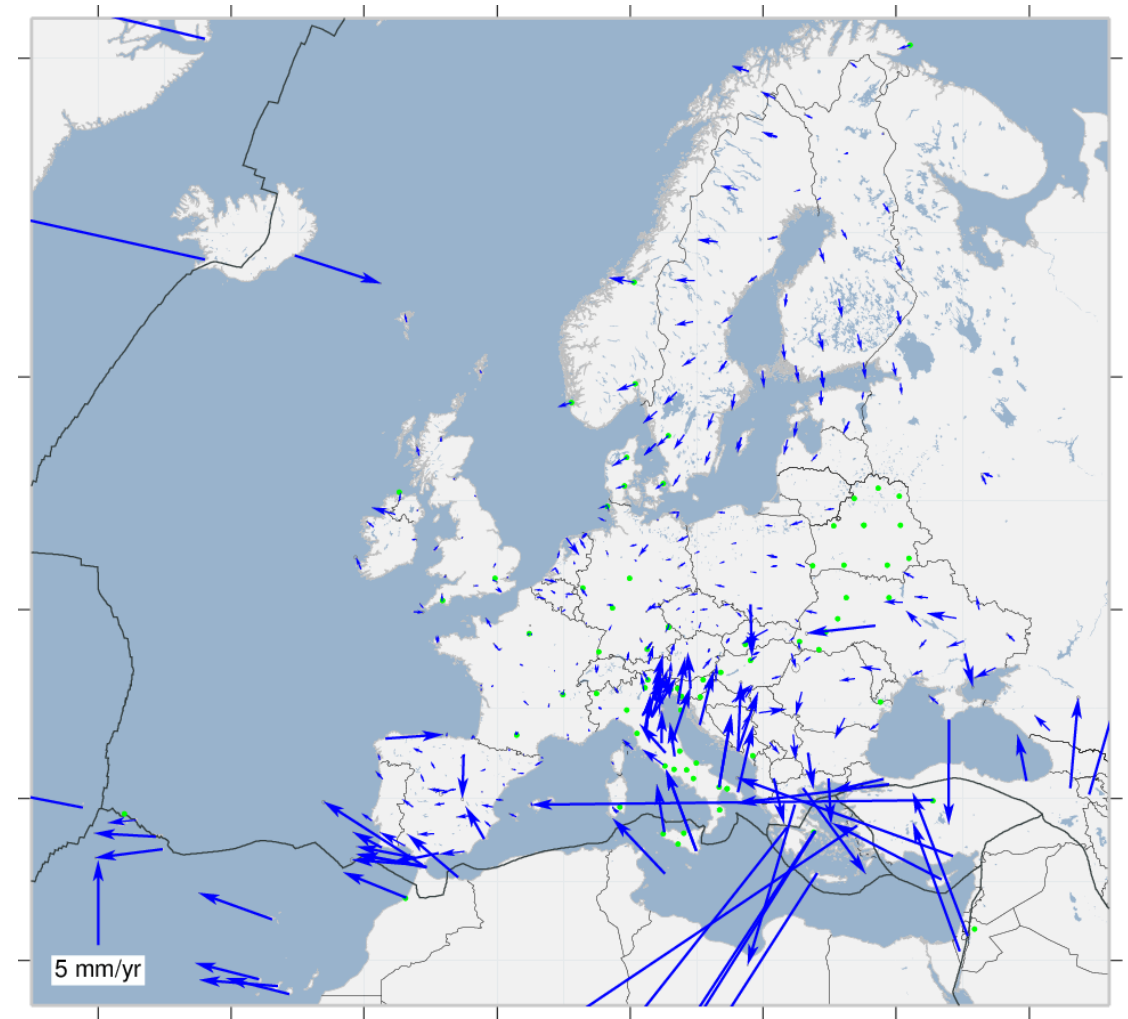
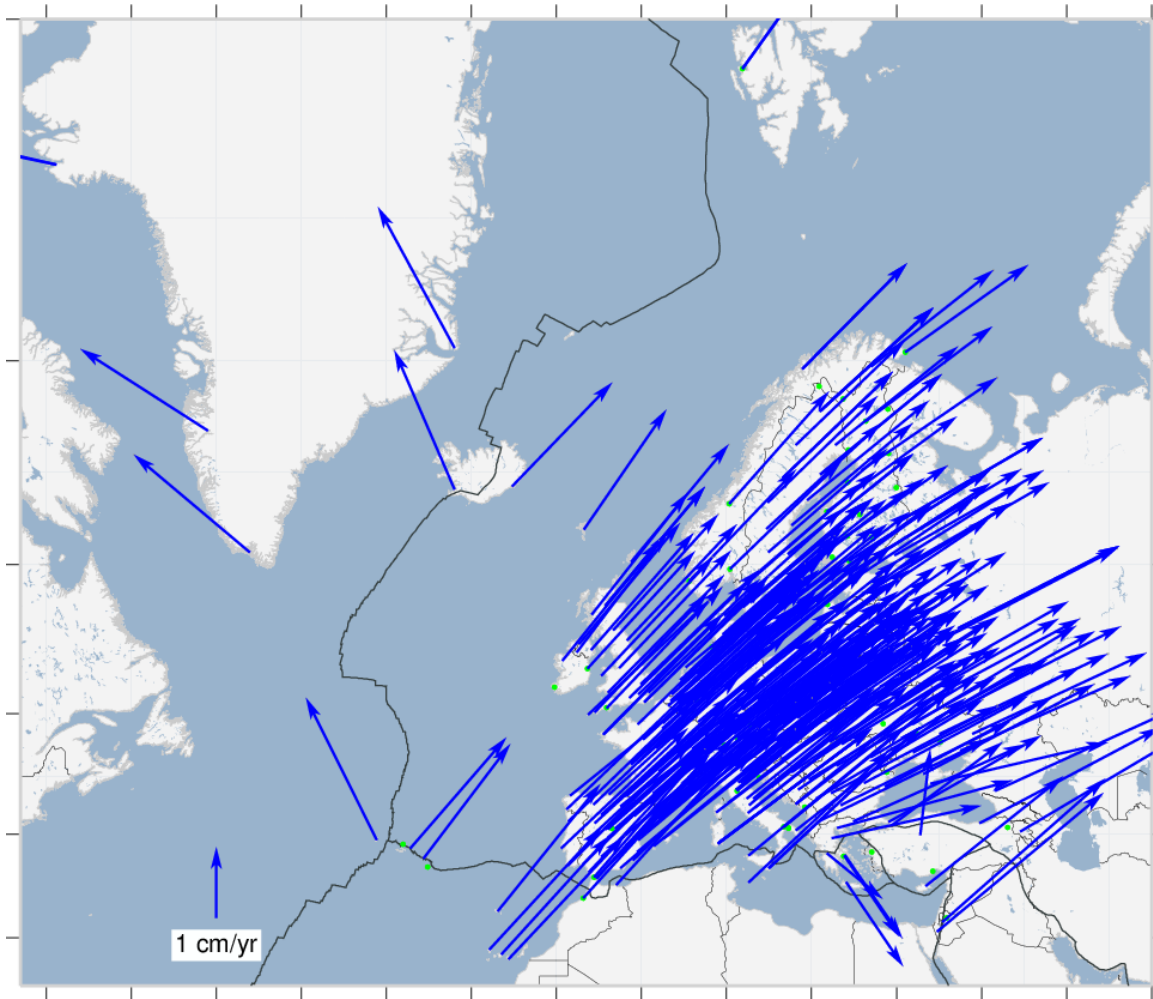


ITRS stations - <https://itrf.ign.fr/en/homepage>



EUREF Permanent GNSS Network: <https://www.epncb.oma.be/index.php>

# Intraplate motion



<https://agupubs.onlinelibrary.wiley.com/doi/full/10.1002/2016JB013098>

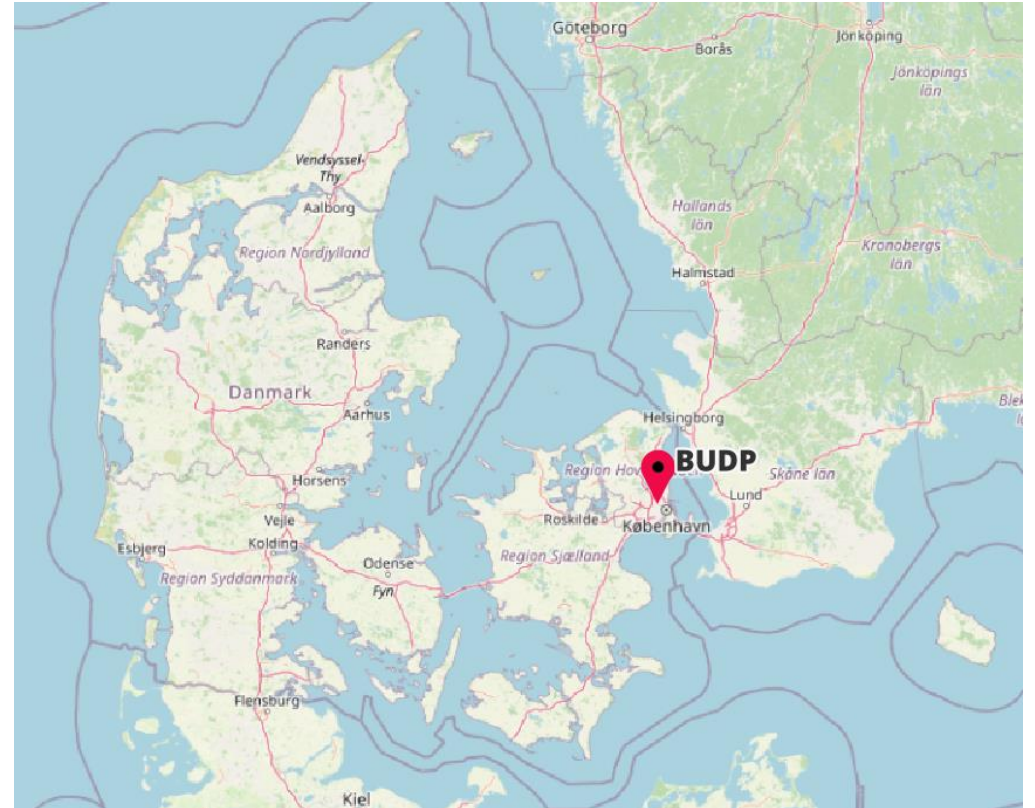
[http://www.epncb.oma.be/\\_productsservices/coordinates/posvel\\_map.php](http://www.epncb.oma.be/_productsservices/coordinates/posvel_map.php)

# Example: Change in position of a Danish reference station

The two reference systems are not equivalent, and have a position bias of approximately 70 cm.

Positions between ITRS and ETRS89DK diverge at a speed of  $\sim 2.5$  cm per year.

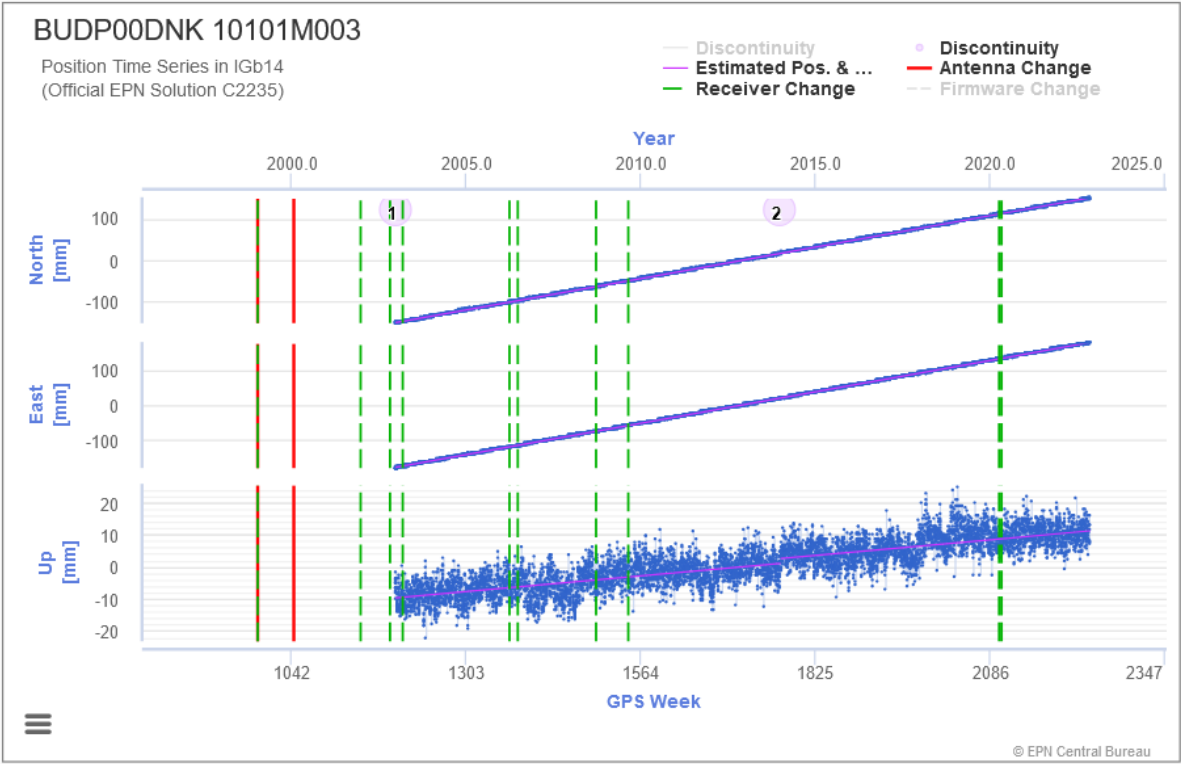
**Example:** Change in positioning of a continuously operating reference station **BUDP** in Copenhagen.



# ITRS vs ETRS89DK

Multi-year Position Time Series of Buddinge reference station in Copenhagen – comparison in 2 datums:

## ➤ ITRS



## ➤ ETRS89



[http://www.epncb.oma.be/\\_productsservices/timeseries/index.php?station=BUDP00DNK&type=ETRS89](http://www.epncb.oma.be/_productsservices/timeseries/index.php?station=BUDP00DNK&type=ETRS89)

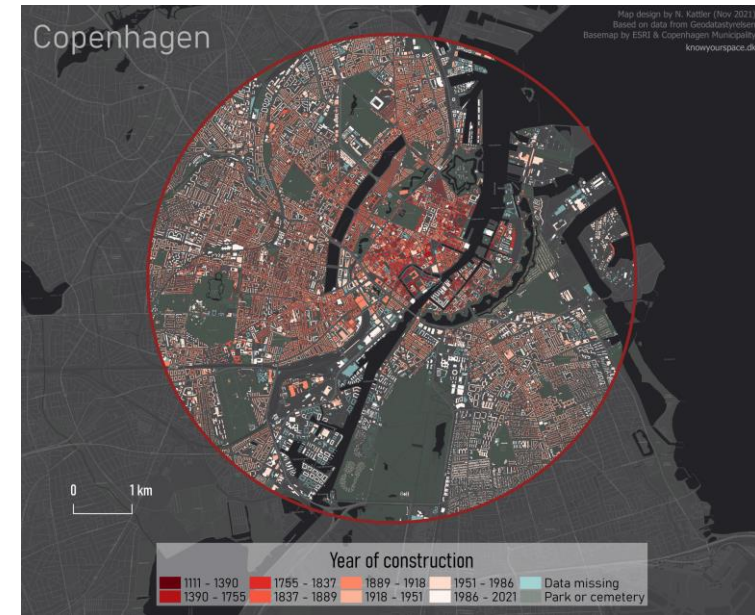
# DANGO Transformations from ITRS to ETRS89DK

- DANGO provides 7 parameters.
- One direct transformation from ITRS to ETRS89DK.
- Parameters can be simply applied using the Helmert transformation formula:

$$\begin{bmatrix} X \\ Y \\ Z \end{bmatrix}_{2015.829}^{ETRF92} = \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}_{2024.192}^{ITRFyy} + \begin{bmatrix} T_1 \\ T_2 \\ T_3 \end{bmatrix} + D \cdot \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}_{2024.192}^{ITRFyy} + \begin{bmatrix} 0 & -R_3 & R_2 \\ R_3 & 0 & -R_1 \\ -R_2 & R_1 & 0 \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}_{2024.192}^{ITRFyy}$$

# DANGO Applications

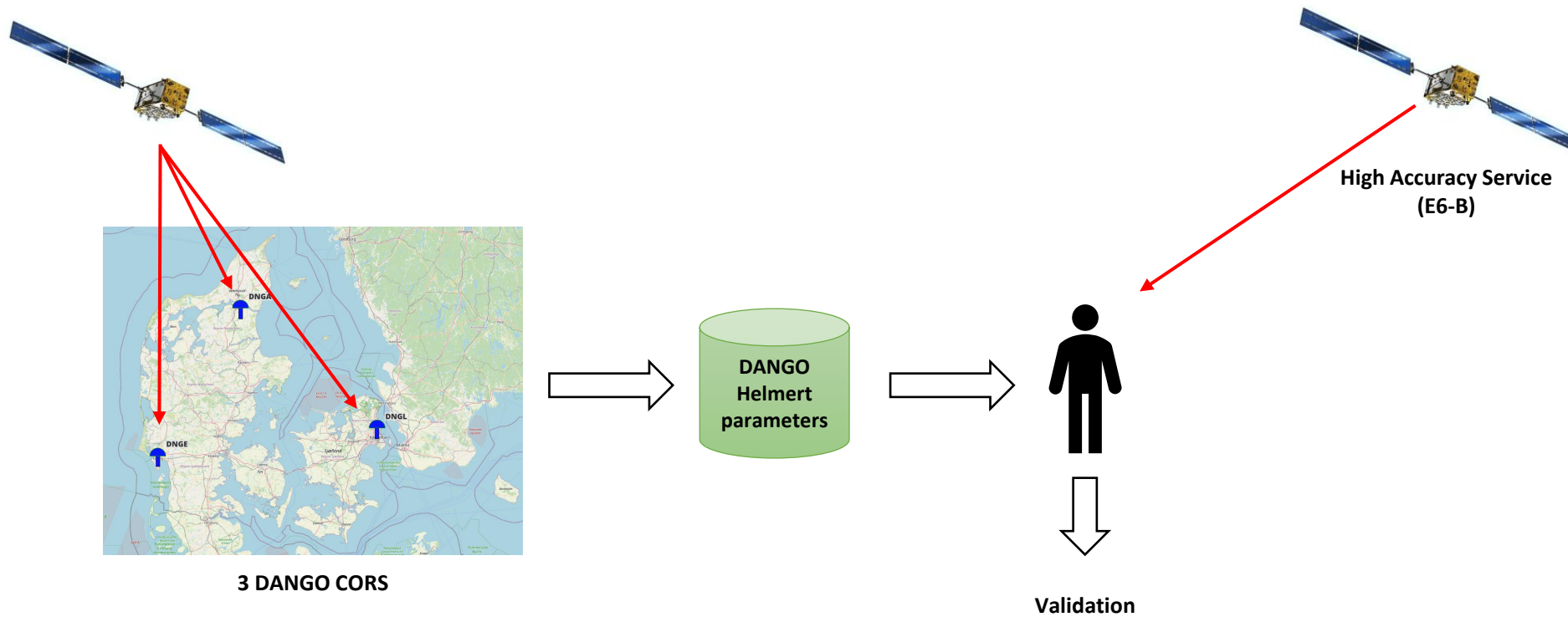
- Why do we want to correct the decimeter-level difference?



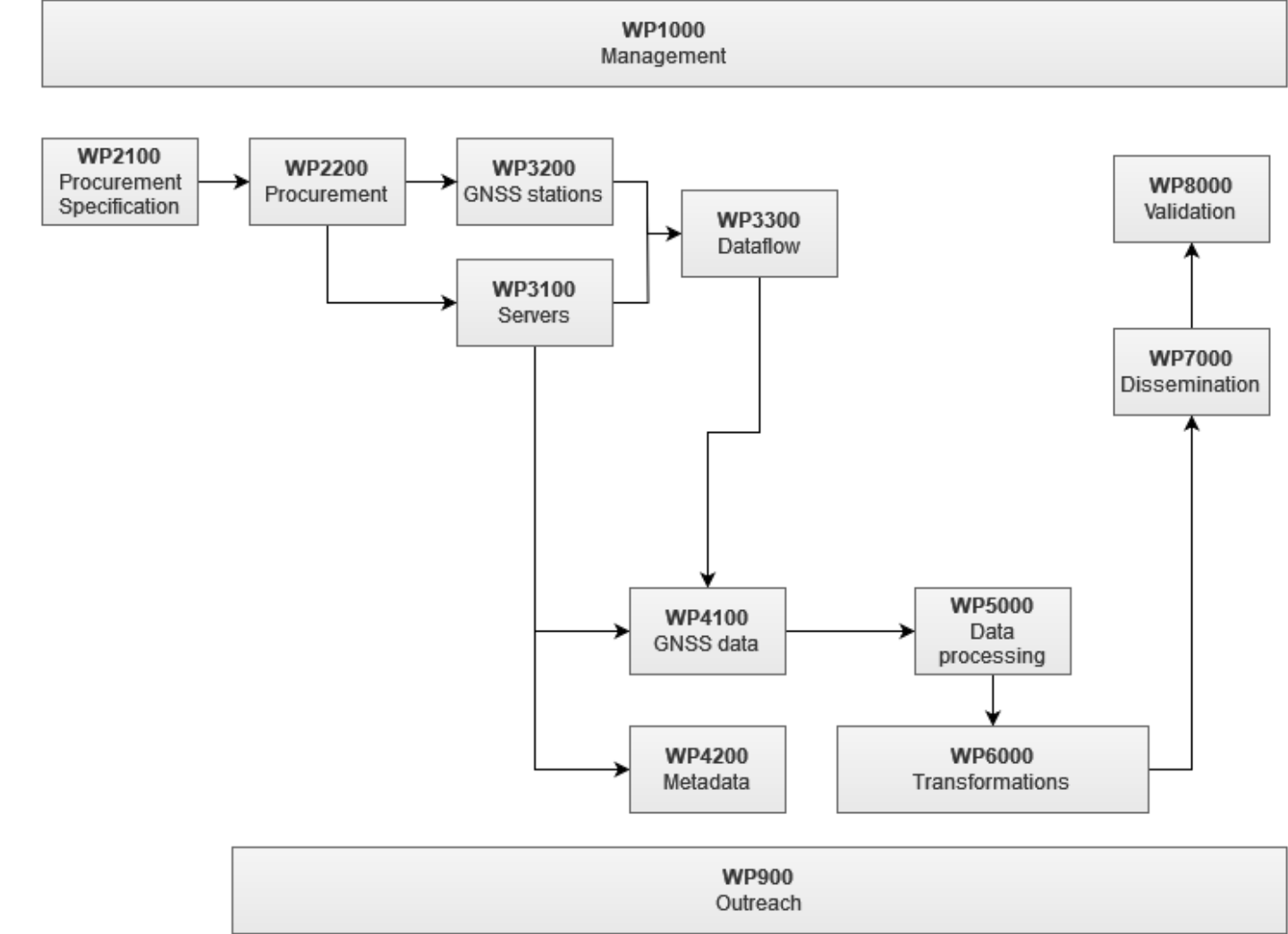
<https://www.space.dtu.dk/english/research-divisions/geomagnetism-and-geospace/research-areas/autonomous-infrastructure>  
<http://www.epncb.oma.be/networkdata/siteinfo4onestation.php?station=BUDD00DNK>  
<https://knowyour.space.dk/2021/11/01/visualising-the-age-of-buildings-copenhagen-ogis/>  
<https://geomatas.com/sistemas-g-n-s-s/>

# Overview of the project structure

# Project work logic



# Project work logic





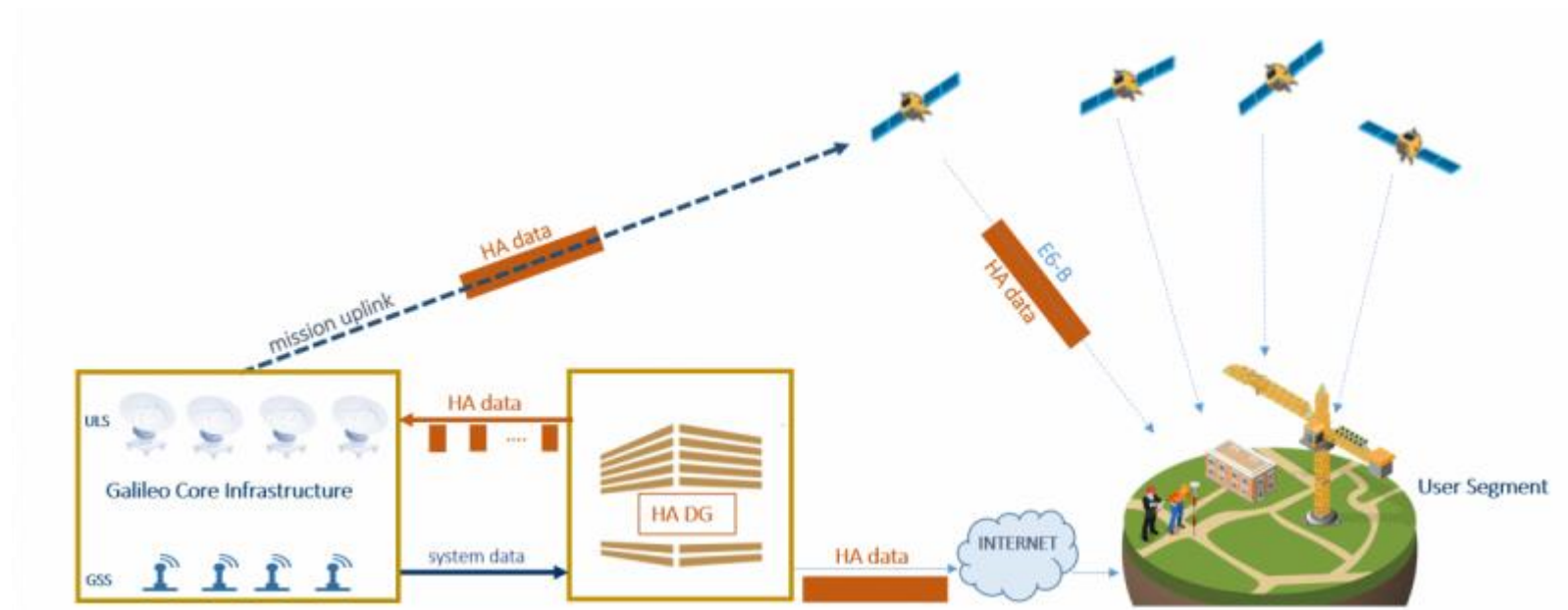
# Methods

# Galileo High Accuracy Service

- Free high accuracy PPP corrections (decimeter level).
- Provided through the Galileo signal E6-B (Signal-In-Space) or through terrestrial means (Internet Data Distribution).
- Galileo HAS corrections must be transformed into ETRS89DK to be used in Denmark.

| Service Level 1 (SL1)                                                              |                           | Service Level 2 (SL2)                                                                                    |
|------------------------------------------------------------------------------------|---------------------------|----------------------------------------------------------------------------------------------------------|
|    | Coverage                  | Global<br>European Coverage Area (ECA)                                                                   |
|    | Corrections               | Orbit, clock, biases (code and phase)<br>Orbit, clock, biases (code and phase) + atmospheric corrections |
|    | Horizontal Accuracy (95%) | <20cm<br><20cm                                                                                           |
|    | Vertical Accuracy (95%)   | <40cm<br><40cm                                                                                           |
|  | Converge Time             | <300s<br><100s                                                                                           |
|  | Availability              | 99%<br>99%                                                                                               |
|  | User HelpDesk             | 24/7<br>24/7                                                                                             |

Target performances for Galileo HAS Service Level 1 (SL1) and Service Level 2 (SL2).



Galileo system elements involved in the generation, provision and exploitation of Galileo HAS.

# Reference frame transformations

- Conventional approach of transforming positions is:
  - 4-step chain of transformations (as used in e.g. PRØJ \*).
  - Using publically available transformation parameters from EUREF.
  - Including the intraplate motion.

$$\text{GTRS} = \text{ITRF2014} (2024.192) \sim \text{ETRF2014} (2024.192) \sim \text{ETRF2014} (2000.0) \sim \text{ETRF92} (2000.0) \sim \text{ETRF92} (2015.829) = \text{ETRS89DK}$$

- DANGO approach is:
  - One direct transformation using DANGO transformation parameters.
  - Intraplate motion not included.

$$\text{GTRS} = \text{ITRF2020} (2024.192) \sim \text{ETRF92} (2015.829) = \text{ETRS89DK}$$

\* PRØJ: <https://proj.org/en/9.5/>

# Conventional approach

Method described in NKG paper and applied in PRØJ can be summarised in 4 steps:

- ITRF2014 @  $t_0 \rightsquigarrow$  ETRF2014 @  $t_0$

$$\begin{bmatrix} X \\ Y \\ Z \end{bmatrix}^{ETRF2014} = \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}_{t_0}^{ITRF2014} + \begin{bmatrix} T_1 \\ T_2 \\ T_3 \end{bmatrix} + \begin{bmatrix} 0 & -\dot{R}_3 & \dot{R}_2 \\ \dot{R}_3 & 0 & -\dot{R}_1 \\ -\dot{R}_2 & \dot{R}_1 & 0 \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}_{t_0}^{ITRF2014} \cdot (t_0 - 1989.0)$$

- ETRF2014 @  $t_0 \rightsquigarrow$  ETRF2014 @ 2000.0

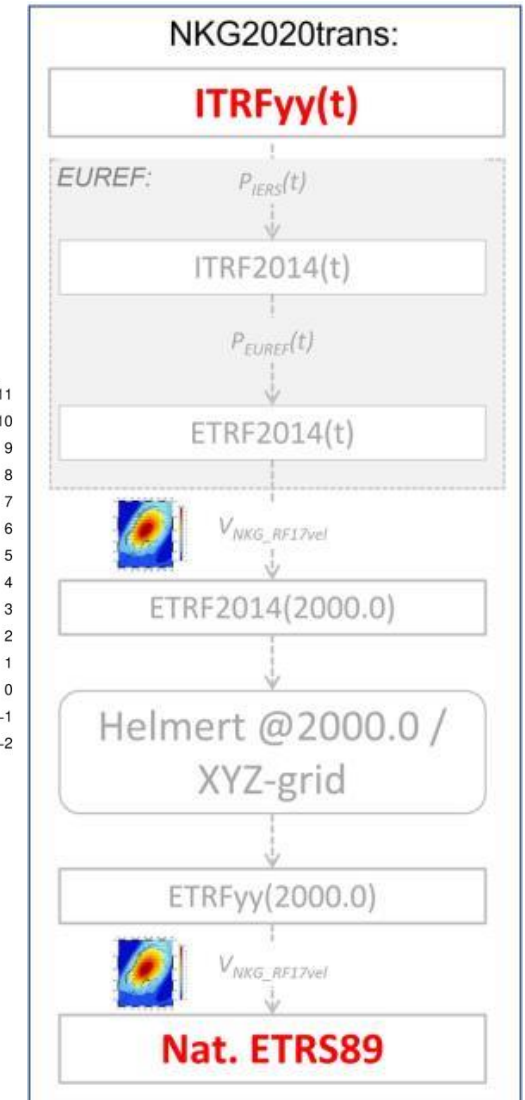
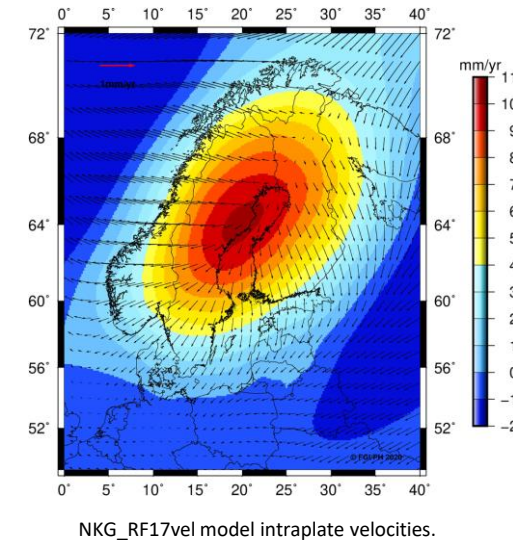
$$\begin{bmatrix} X \\ Y \\ Z \end{bmatrix}_{2000.0}^{ETRF2014} = \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}_{t_0}^{ETRF2014} + (2000.0 - t_0) \cdot \begin{bmatrix} V_{X,intra} \\ V_{Y,intra} \\ V_{Z,intra} \end{bmatrix}_{NKG\_RF17vel}^{ETRF2014}$$

- ETRF2014 @ 2000.0  $\rightsquigarrow$  ETRF92 @ 2000.0

$$\begin{bmatrix} X \\ Y \\ Z \end{bmatrix}_{2000.0}^{ETRF92} = \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}_{2000.0}^{ETRF2014} + \begin{bmatrix} T_1 \\ T_2 \\ T_3 \end{bmatrix} + D \cdot \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}_{2000.0}^{ETRF2014} + \begin{bmatrix} 0 & -R_3 & R_2 \\ R_3 & 0 & -R_1 \\ -R_2 & R_1 & 0 \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}_{2000.0}^{ETRF2014}$$

- ETRF92 @ 2000.0  $\rightsquigarrow$  ETRF92 @ 2015.829

$$\begin{bmatrix} X \\ Y \\ Z \end{bmatrix}_{t_c}^{ETRF92} = \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}_{2000.0}^{ETRF92} + (t_c - 2000.0) \cdot \begin{bmatrix} V_{X,intra} \\ V_{Y,intra} \\ V_{Z,intra} \end{bmatrix}_{NKG\_RF17vel}^{ETRF2014}$$



NKG2020 transformation method and the associated steps.

# Transformation parameters

➤ Example transformation parameters from EUREF Technical Note:

Table 3: Transformation parameters from ITRF<sub>yy</sub> to ETRF2014 at epoch 2015.0 and their rates/year

| ITRF Solution | T1<br>mm | T2<br>mm | T3<br>mm | D<br>10 <sup>-9</sup> | R1<br>mas | R2<br>mas | R3<br>mas |
|---------------|----------|----------|----------|-----------------------|-----------|-----------|-----------|
| ITRF2020      | -1.4     | -0.9     | 1.4      | -0.42                 | 2.210     | 13.806    | -20.020   |
| rates         | 0.0      | -0.1     | 0.2      | 0.00                  | 0.085     | 0.531     | -0.770    |
| ITRF2014      | 0.0      | 0.0      | 0.0      | 0.00                  | 2.210     | 13.806    | -20.020   |
| rates         | 0.0      | 0.0      | 0.0      | 0.00                  | 0.085     | 0.531     | -0.770    |
| ITRF2008      | -1.6     | -1.9     | -1.9     | -0.13                 | 2.210     | 13.806    | -20.020   |
| rates         | 0.0      | 0.0      | 0.1      | -0.03                 | 0.085     | 0.531     | -0.770    |
| ITRF2005      | -4.1     | -1.0     | 2.8      | -1.07                 | 2.210     | 13.806    | -20.020   |
| rates         | -0.3     | 0.0      | 0.1      | -0.03                 | 0.085     | 0.531     | -0.770    |
| ITRF2000      | -1.2     | -1.7     | 35.6     | -2.67                 | 2.210     | 13.806    | -20.020   |
| rates         | -0.1     | -0.1     | 1.9      | -0.11                 | 0.085     | 0.531     | -0.770    |
| ITRF97        | -7.9     | 3.0      | 79.3     | -4.40                 | 2.210     | 13.806    | -20.380   |
| rates         | -0.1     | 0.5      | 3.3      | -0.12                 | 0.085     | 0.531     | -0.790    |
| ITRF96        | -7.9     | 3.0      | 79.3     | -4.40                 | 2.210     | 13.806    | -20.380   |
| rates         | -0.1     | 0.5      | 3.3      | -0.12                 | 0.085     | 0.531     | -0.790    |
| ITRF94        | -7.9     | 3.0      | 79.3     | -4.40                 | 2.210     | 13.806    | -20.380   |
| rates         | -0.1     | 0.5      | 3.3      | -0.12                 | 0.085     | 0.531     | -0.790    |
| ITRF93        | 64.4     | -2.8     | 72.7     | -4.89                 | 5.570     | 18.136    | -20.770   |
| rates         | 2.8      | 0.1      | 2.5      | -0.12                 | 0.195     | 0.721     | -0.840    |
| ITRF92        | -15.9    | 1.0      | 87.3     | -3.69                 | 2.210     | 13.806    | -20.380   |
| rates         | -0.1     | 0.5      | 3.3      | -0.12                 | 0.085     | 0.531     | -0.790    |
| ITRF91        | -27.9    | -13.0    | 93.3     | -5.09                 | 2.210     | 13.806    | -20.380   |
| rates         | -0.1     | 0.5      | 3.3      | -0.12                 | 0.085     | 0.531     | -0.790    |
| ITRF90        | -25.9    | -9.0     | 109.3    | -5.39                 | 2.210     | 13.806    | -20.380   |
| rates         | -0.1     | 0.5      | 3.3      | -0.12                 | 0.085     | 0.531     | -0.790    |
| ITRF89        | -30.9    | -33.0    | 147.3    | -8.79                 | 2.210     | 13.806    | -20.380   |
| rates         | -0.1     | 0.5      | 3.3      | -0.12                 | 0.085     | 0.531     | -0.790    |

Altamimi et al. 2024, EUREF Technical Note 1: Relationship and Transformation between the International and the European Terrestrial Reference Systems. <http://etrs89.ensg.ign.fr/pub/EUREF-TN-1-Mar-04-2024.pdf>

# DANGO Transformations from ITRS to ETRS89DK

- DANGO provides 7 parameters.
- One direct transformation from ITRS to ETRS89DK.
- Parameters can be simply applied using the Helmert transformation formula:

$$\begin{bmatrix} X \\ Y \\ Z \end{bmatrix}_{2015.829}^{ETRF92} = \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}_{2024.192}^{ITRFyy} + \begin{bmatrix} T_1 \\ T_2 \\ T_3 \end{bmatrix} + D \cdot \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}_{2024.192}^{ITRFyy} + \begin{bmatrix} 0 & -R_3 & R_2 \\ R_3 & 0 & -R_1 \\ -R_2 & R_1 & 0 \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}_{2024.192}^{ITRFyy}$$

# DANGO CORS

In order to obtain 7 parameters, data from at least three reference stations is required.

As part of DANGO, three permanent CORS were established in:

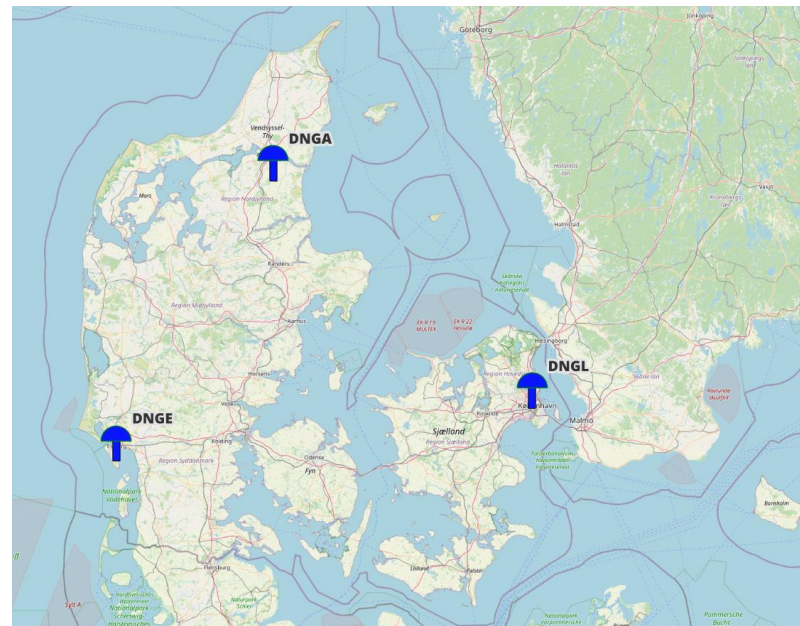
- Lyngby (DNGL)
- Esbjerg (DNGE)
- Aalborg (DNGA)

Equipment:

- Septentrio PolaRx5s GNSS receiver
- Leica LEIAR20 LEIM antenna

The data is accessible through the SFTP data infrastructure.

The stations will continue operating and will be maintained by the universities.

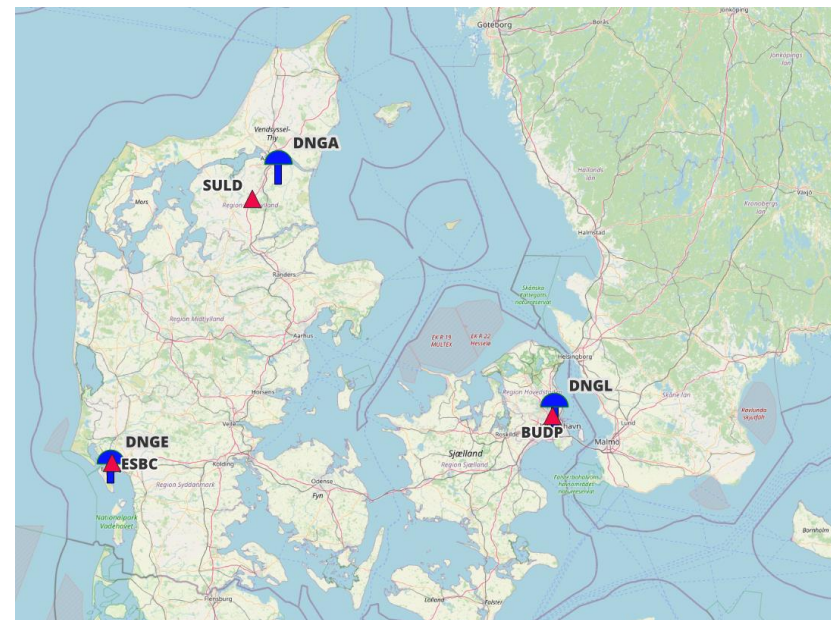


# DANGO CORS positioning

- Obtaining precise positions of the 3 DANGO stations
- Positions have to be in **both ITRS and ETRS89DK**
- Method: **Post Processing Kinematic (PPK)**
  - Data from the DANGO stations
  - Data from Danish CORS with the shortest baselines.
  - Novatel Inertial Explorer
  - 24h 1Hz timeseries
  - Double-frequency mixed observation RINEX3 files.

Stations were paired as following (shortest baselines):

- DNGL + BUDP
- DNGL + ESBC
- DNGL + SULD



# DANGO Transformation parameters

- 7 Helmert parameters.
- Derived using least squares adjustment\*.

|                       | ITRS -> ETRS89DK |
|-----------------------|------------------|
| T <sub>x</sub> [mm]   | 876.599          |
| T <sub>y</sub> [mm]   | -76.52           |
| T <sub>z</sub> [mm]   | -626.228         |
| D [10 <sup>-9</sup> ] | 2.197            |
| R <sub>x</sub> [mas]  | 2.878            |
| R <sub>y</sub> [mas]  | -14.102          |
| R <sub>z</sub> [mas]  | -20.630          |

$$\begin{bmatrix} X \\ Y \\ Z \end{bmatrix}_{2015.829}^{ETRF92} = \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}_{2024.192}^{ITRFyy} + \begin{bmatrix} T_1 \\ T_2 \\ T_3 \end{bmatrix} + D \cdot \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}_{2024.192}^{ITRFyy} + \begin{bmatrix} 0 & -R_3 & R_2 \\ R_3 & 0 & -R_1 \\ -R_2 & R_1 & 0 \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}_{2024.192}^{ITRFyy}$$

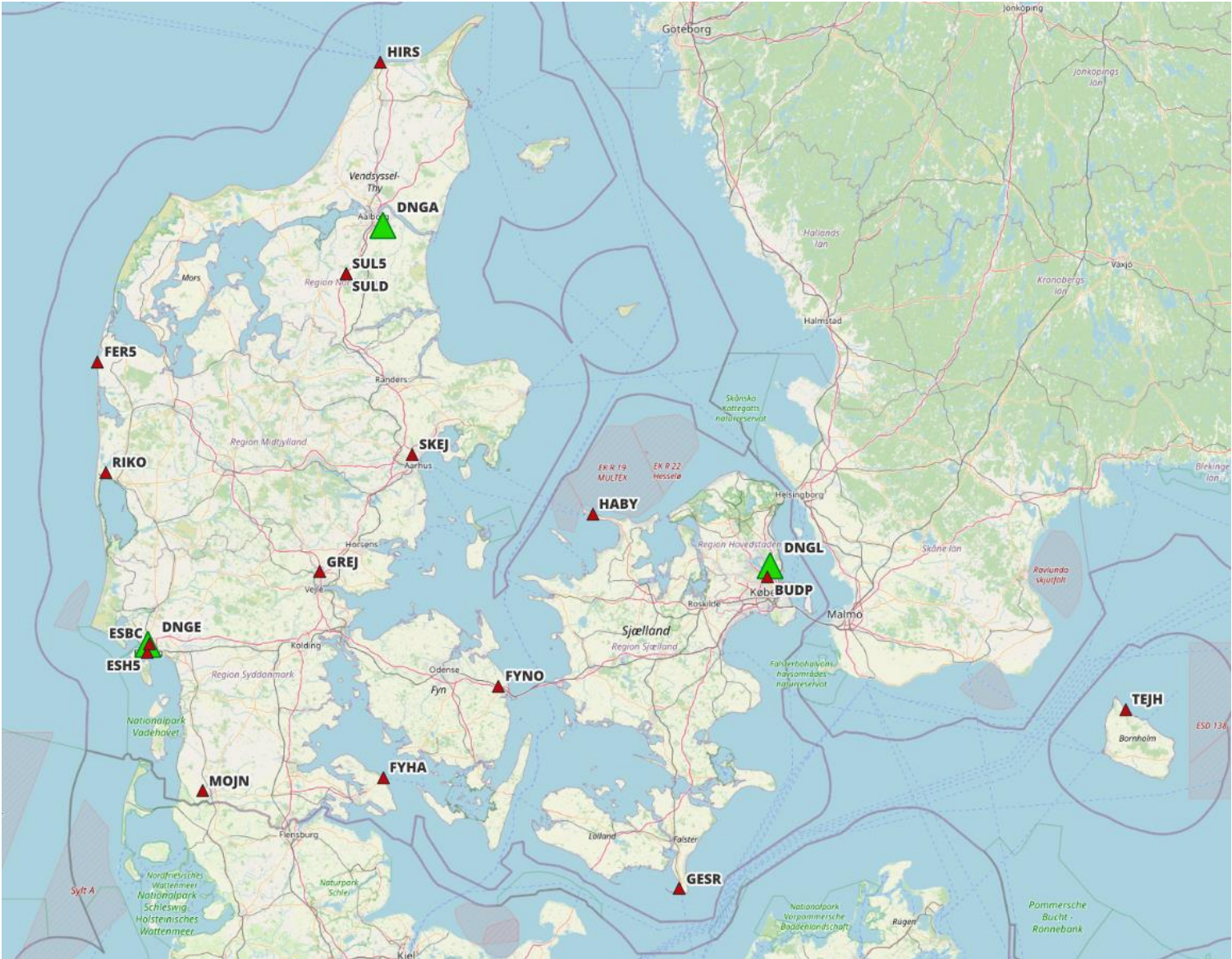
\* As described in: Altamimi, Z., Sillard, P., Boucher, C., (2002) ITRF2000: A new release of the International Terrestrial Reference Frame for earth science applications. <https://agupubs.onlinelibrary.wiley.com/doi/10.1029/2001JB000561>

# Validation of DANGO parameters

# DANGO Validation

- Using known positions of the National CORS network of 16 stations.
- Using known positions of the TAPAS network.
- Evaluation is based on residuals between the known station coordinates in ETRS89DK and the coordinates transformed from ITRS into ETRS89DK.

# Danish National CORS and DANGO CORS

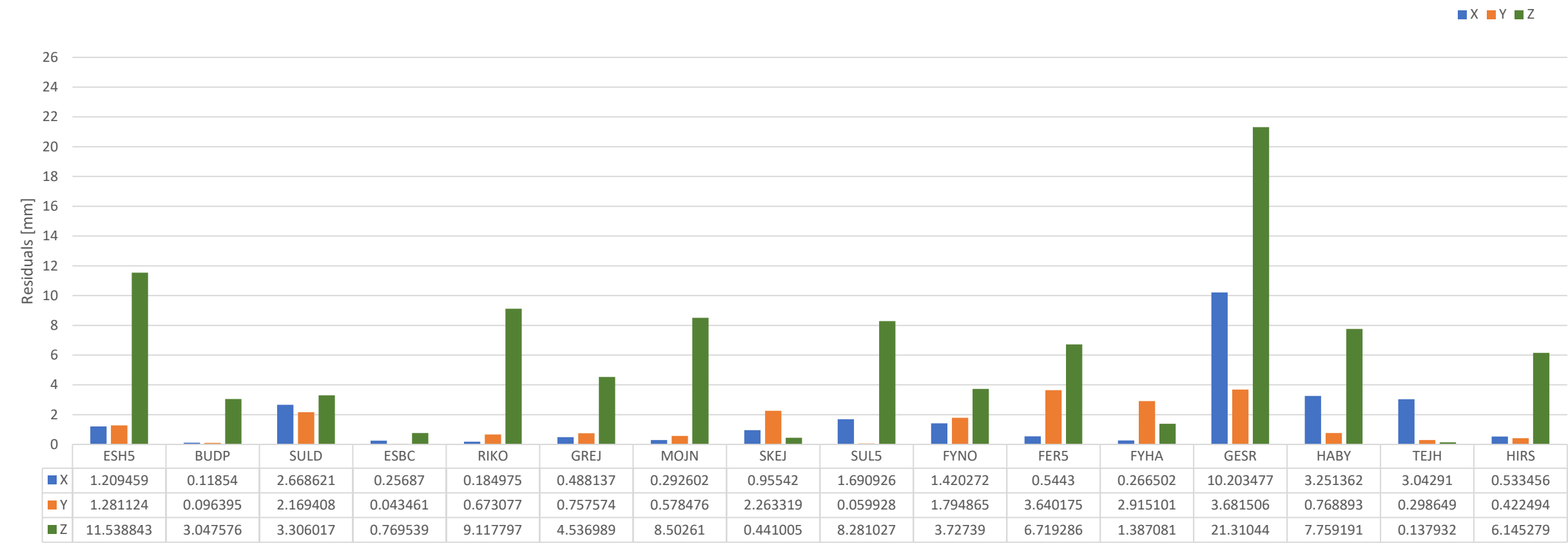


# Validation using Danish National CORS

➤ Based on known coordinates of 16 Danish National CORS in **ITRS** and **ETRS89DK**.

**ITRF2020 @ 2024.192 ~ ETRS89DK**

CORS residuals

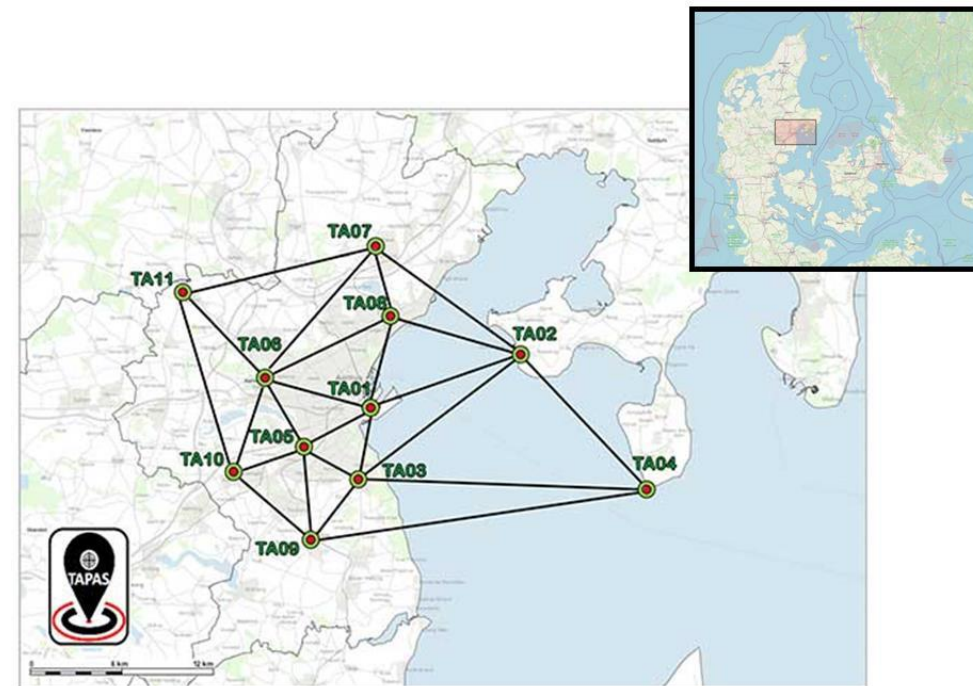
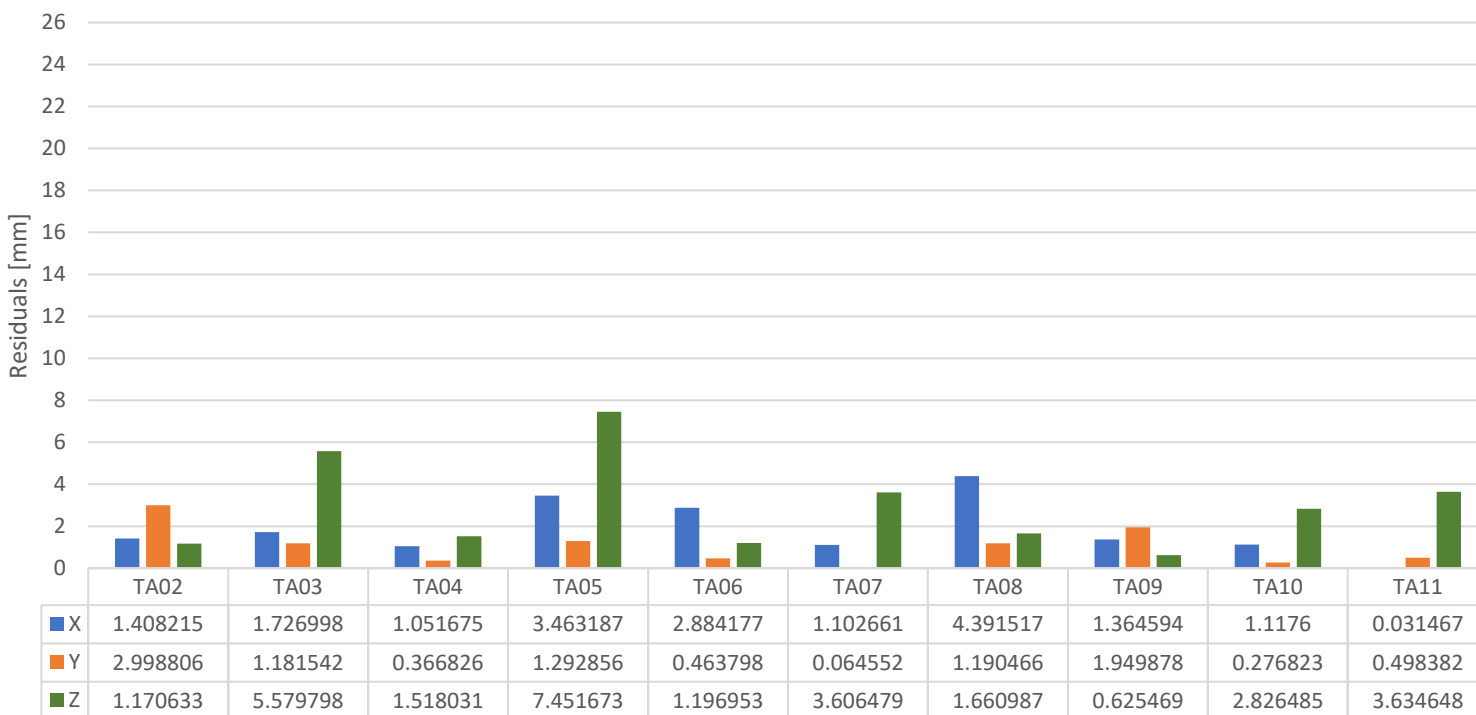


# Validation using TAPAS stations

- TAPAS positions in ETRS89DK were given at an epoch 2020.19.
- Transformations use ETRF92@2015.829

TAPAS residuals

■ X ■ Y ■ Z



# Result dissemination

# Data dissemination - Utilizing NTRIP with RTCM

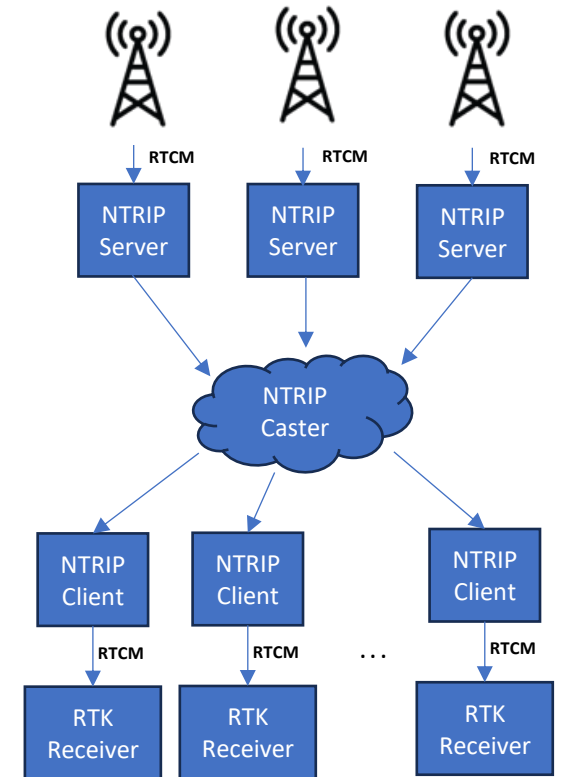
Originally, open standards like NTRIP and RTCM were planned to be used for dissemination of the Helmert transformation parameters.

The following RTCM were chosen:

- 1021 – Helmert Transformation Parameters
- 1023 – Residuals, Ellipsoidal Grid Representation

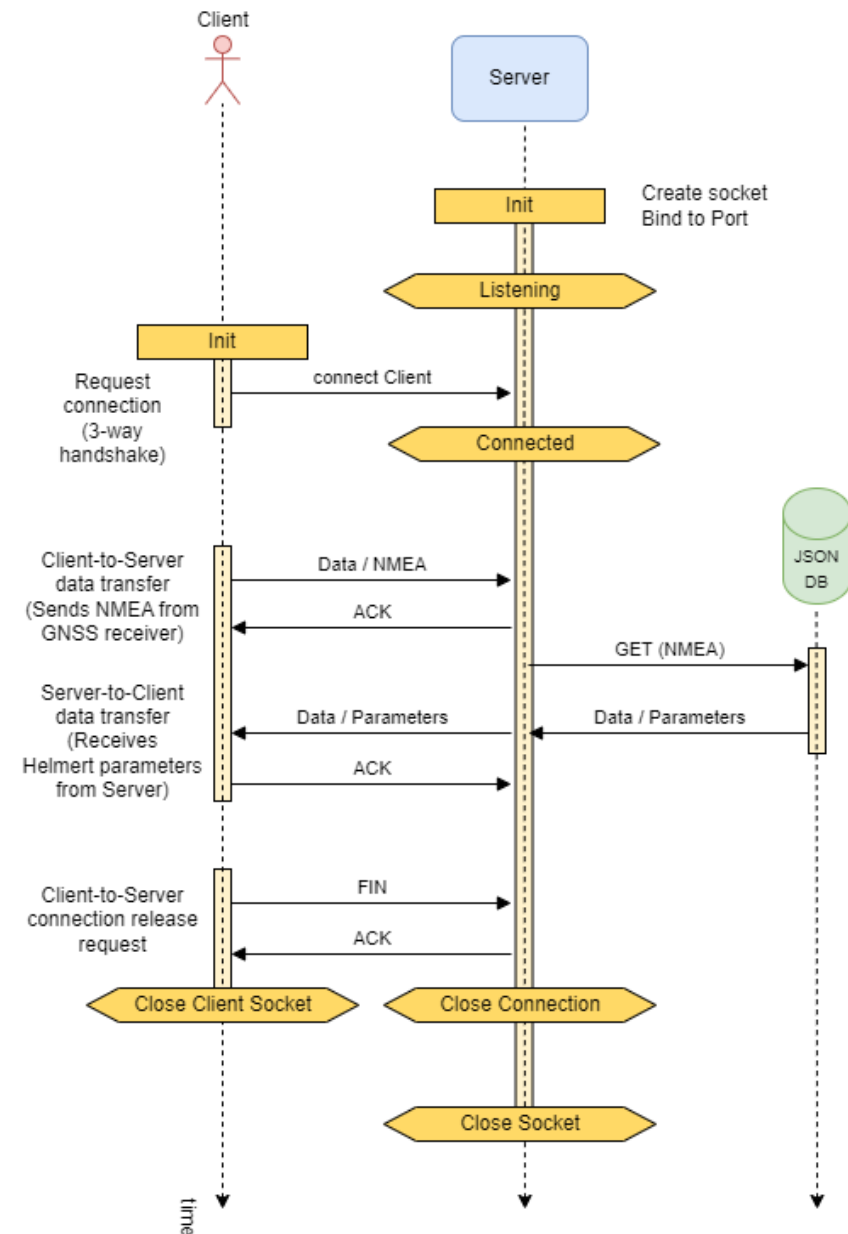
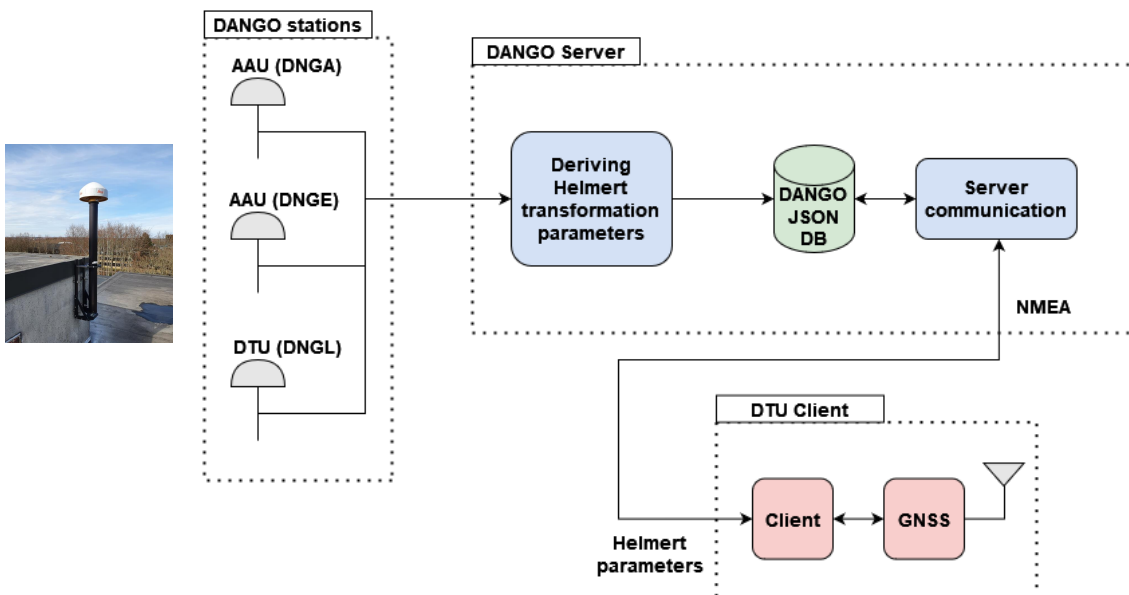
However, these are not found in actual use and they are not implemented for receivers.

- Could implement RTCM encoder/decoder as replacement, but this was outside of the scope of DANGO.



# DANGO dissemination

- TCP/IP Client-Server structure.
- 7 Helmert parameters saved in a JSON file.
- JSON stored on the Server side.
- Client requests the parameters from the Server.
- Client can use the parameters to carry out transformations in real-time.



# Demo example – TCP/IP System

In [ ]:

In [ ]:

In [ ]:

In [ ]:

In [ ]:

In [ ]:

In [ ]:

```
Initiating Server
Server socket is binded to port: 1111
Socket is listening . . .
```

IPython ConsoleHistory

conda (Python 3.11.4) Completions: conda ✓ LSP: Python Line 8, Col 1 ASCII CRLF RW Mem 65%

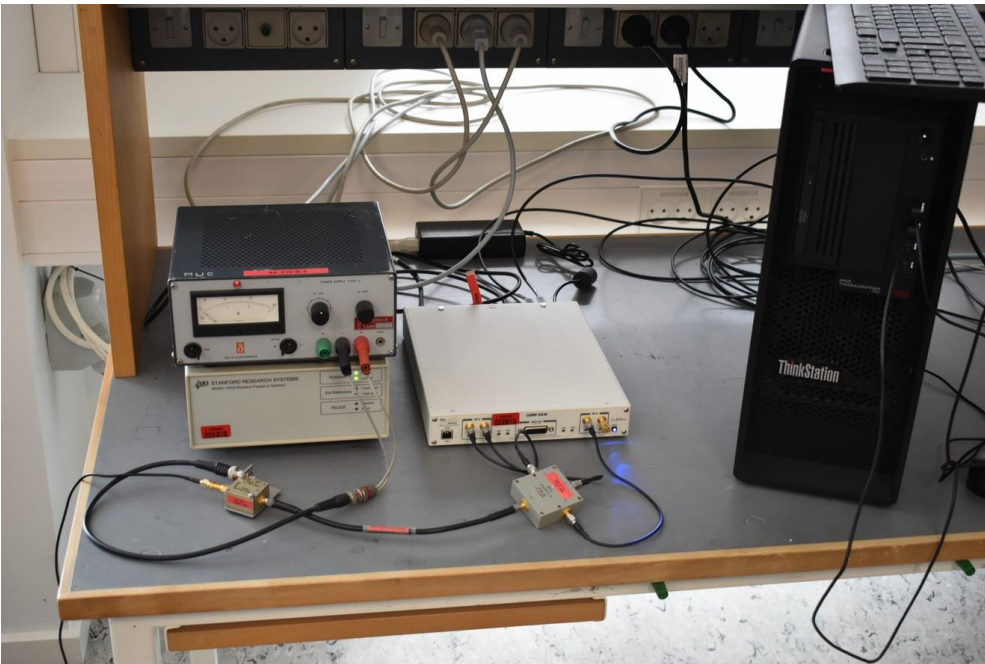
Client

Server

# HAS signals and DANGO

# Utilizing the HAS signals with DANGO

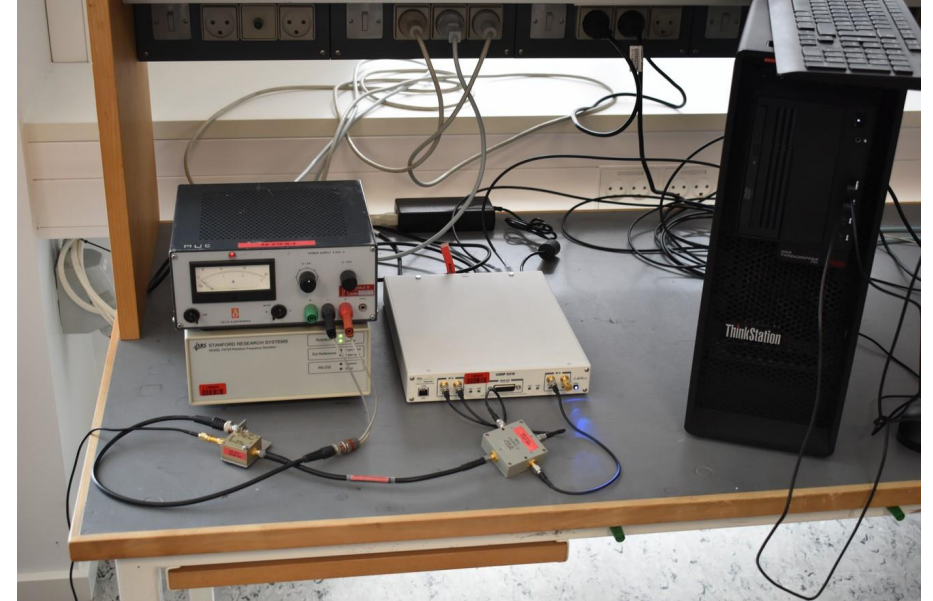
- HAS messages were extracted using Software Defined Receiver (SDR) data stream.
- HAS was utilized with the new HAS-capable GNSS receiver: EOS Arrow Gold+



# System for capturing data stream with SDR

Hardware:

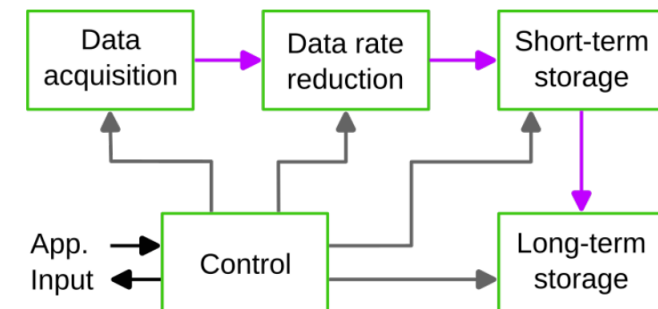
- Ettus Research X310 Software-Defined Radio (SDR)
  - Receives GNSS signals via antenna
  - Performs down-conversion from RF frequency range to baseband
  - Samples the baseband signal, I/Q data
  - Transfers data to host computer.



Hardware setup

Software for capture and storage consists of modules:

- Data acquisition
- Data rate reduction
- Short-term storage (FIFO)
- Long-term storage
- Control



Module structure

# HAS message decoding

Status of the HAS decoding:

- Installed, configured, tested on the SDR platform.
- HAS messages successfully extracted.

Next steps:

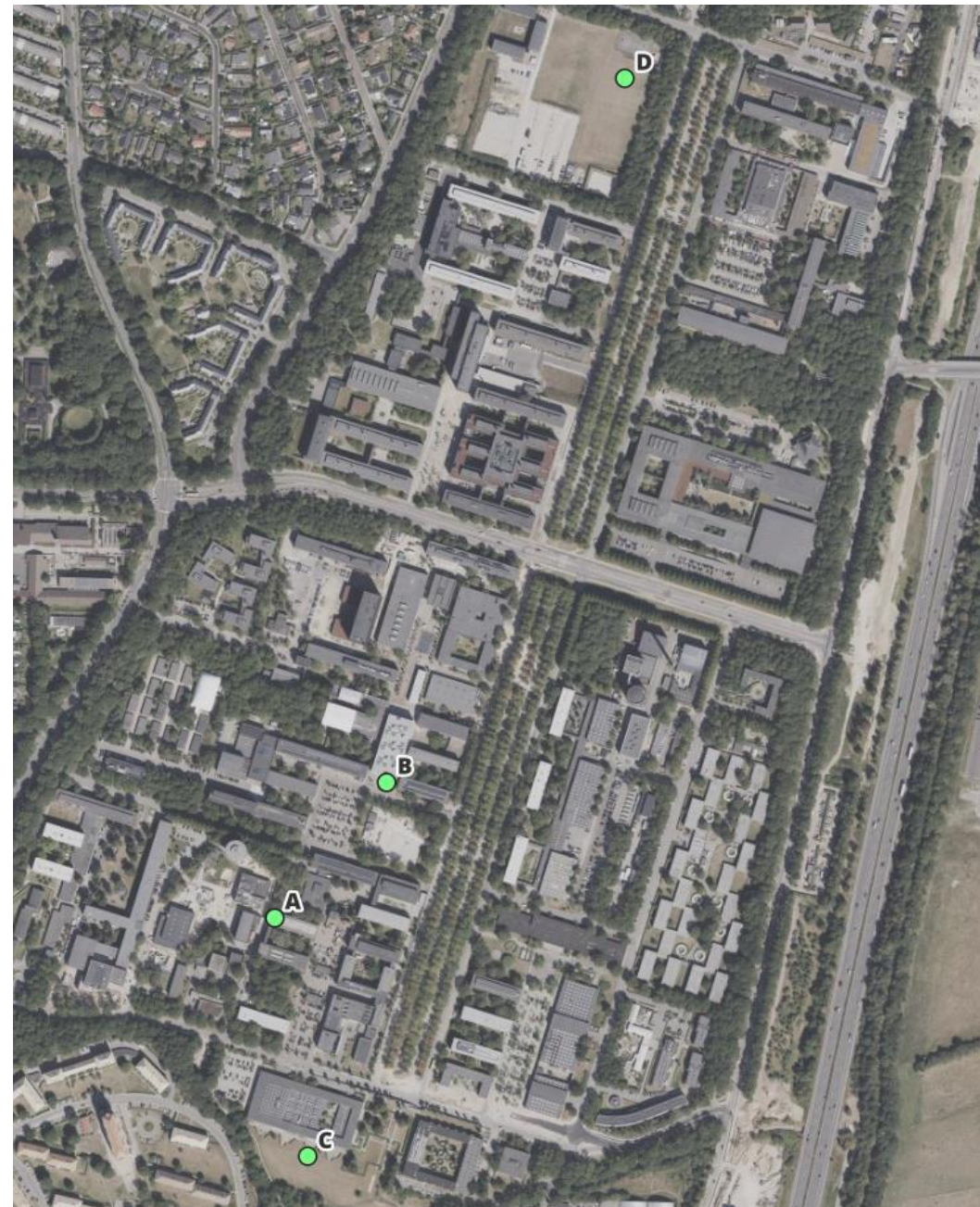
- Output HAS messages as RTCM messages.
- Use SDR platform for channel sounding/sensing.

# In-situ tests with EOS Arrow Gold+

Various tests were carried out with the EOS Arrow Gold+ GNSS receiver to test its performance.

Comparison of performance in different conditions:

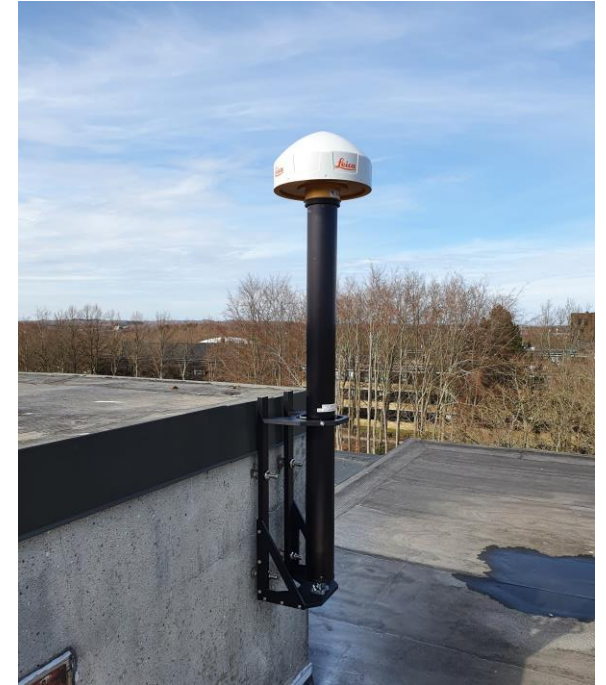
- A - Rooftop LEIAR20 LEIM antenna (ideal conditions)
- B - Urban conditions (EOS antenna)
- C - Semi-urban conditions (EOS antenna)
- D - Kinematic test (EOS antenna)



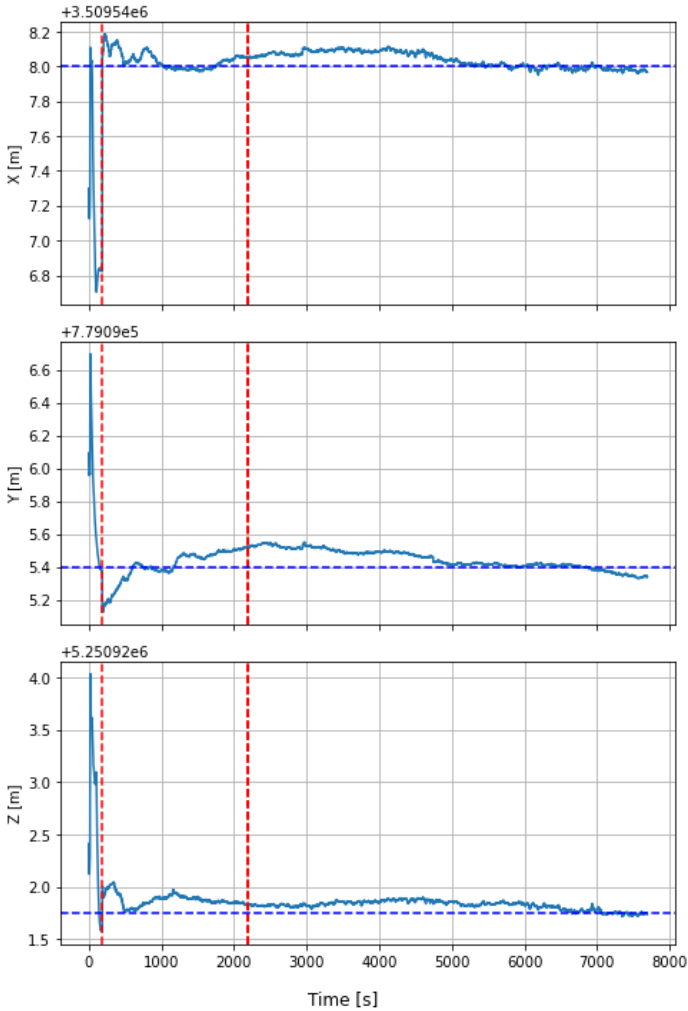
Aerial image of DTU and locations of 4 in-situ tests.

# Rooftop tests

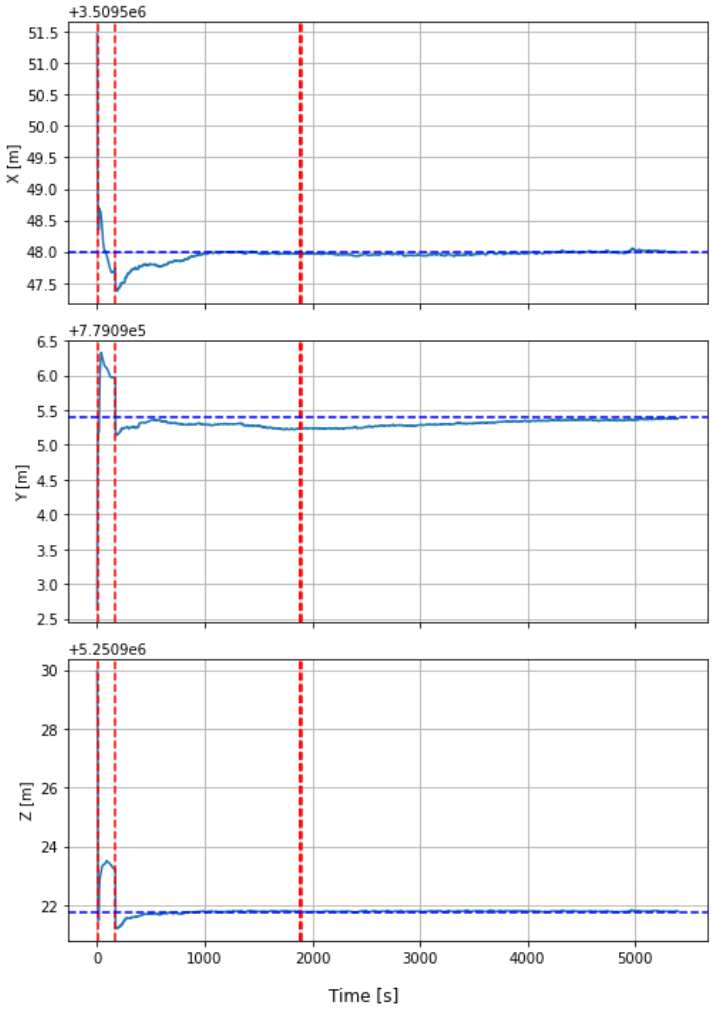
- Location A (Building 348, same location as DNGL)
- Connected Arrow to the DNGL antenna with a splitter.
- Unobstructed view of the sky from high location with no obstacles.
- 3 tests were carried out during different times of day.
- Since the precise position of DNGL is known, it can be used to verify accuracy of the static tests with Arrow.



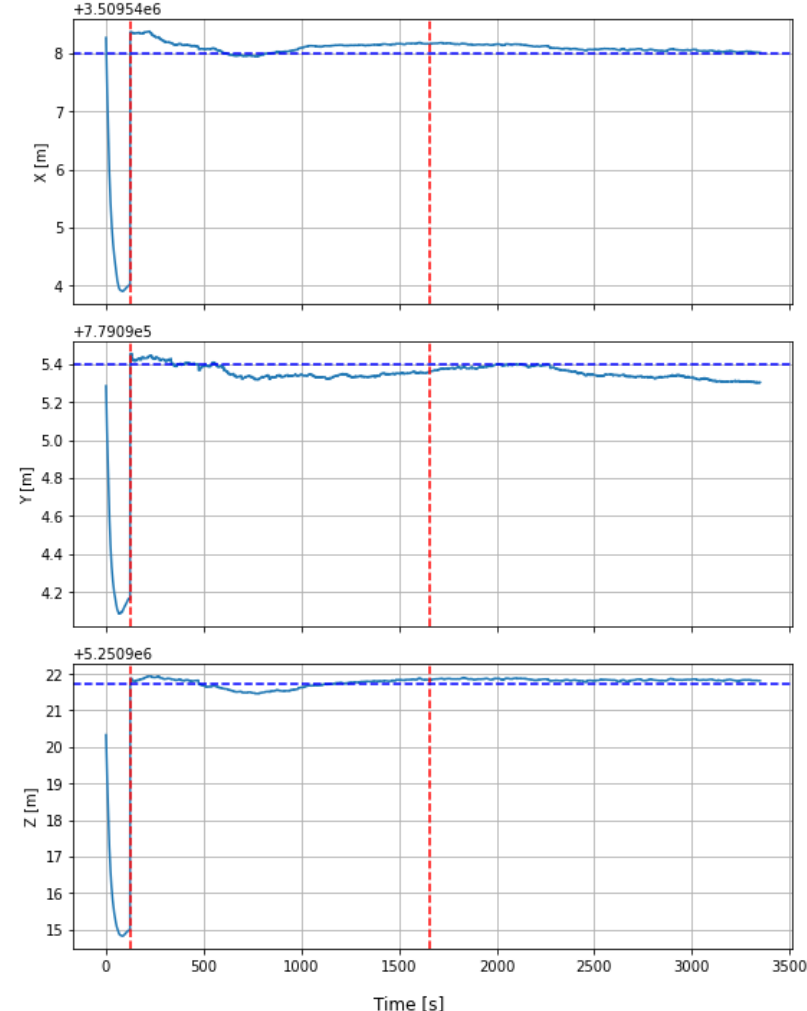
# Rooftop tests



GALHAS FIX achieved after: 36.6 minutes



GALHAS FIX achieved after: 31.67 minutes



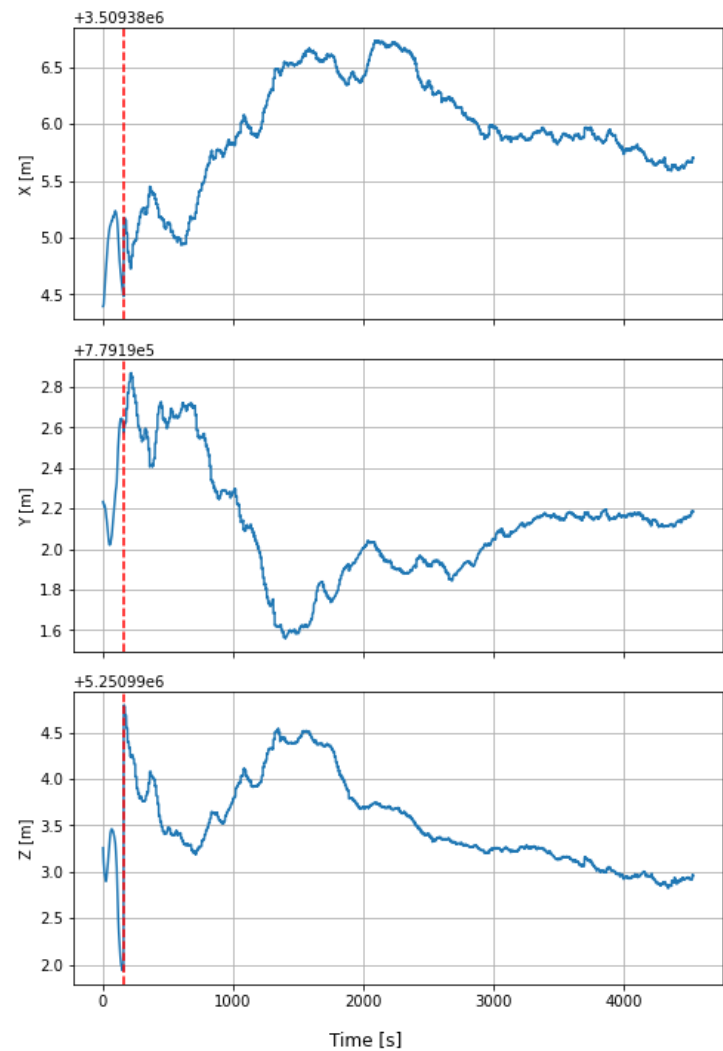
GALHAS FIX achieved after: 27.57 minutes

# Urban conditions

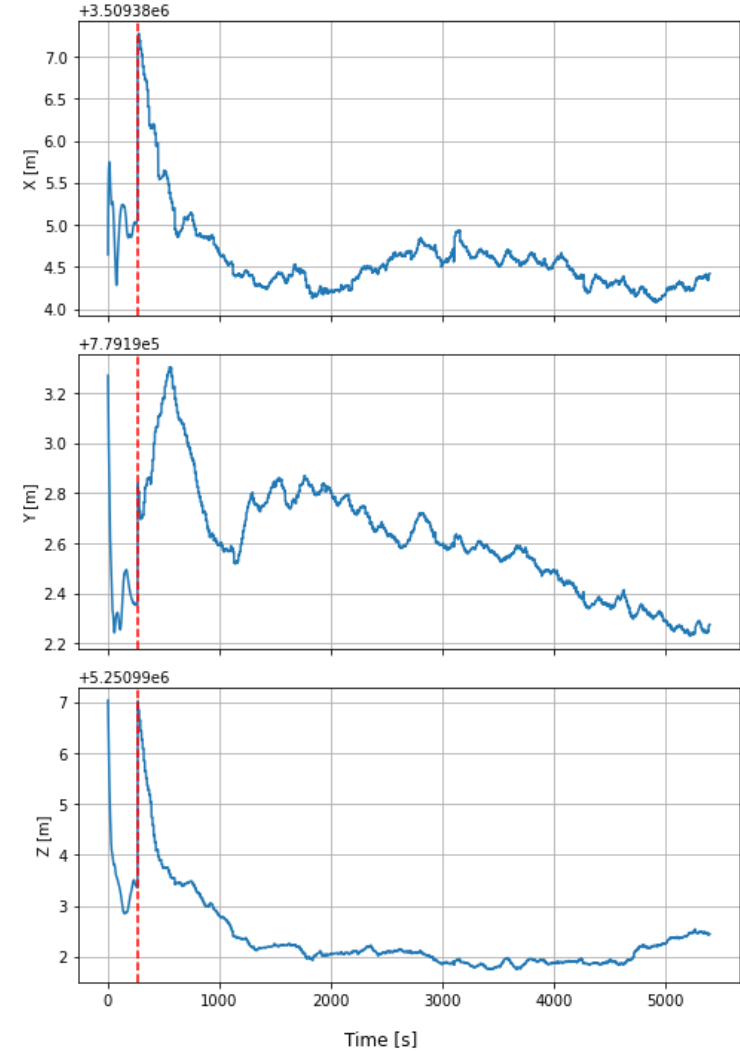
- Location B (Urban location with trees and tall buildings nearby).
- Connected Arrow to the EOS antenna placed on a tripod.
- Very limited view of the sky from a ground location.
- 2 tests were carried out during different times of day.
- Tests were carried out to see if Galileo HAS Float/Fixed status can be achieved in difficult conditions.



# Urban conditions



GALHAS FLT achieved after: 2.63 minutes



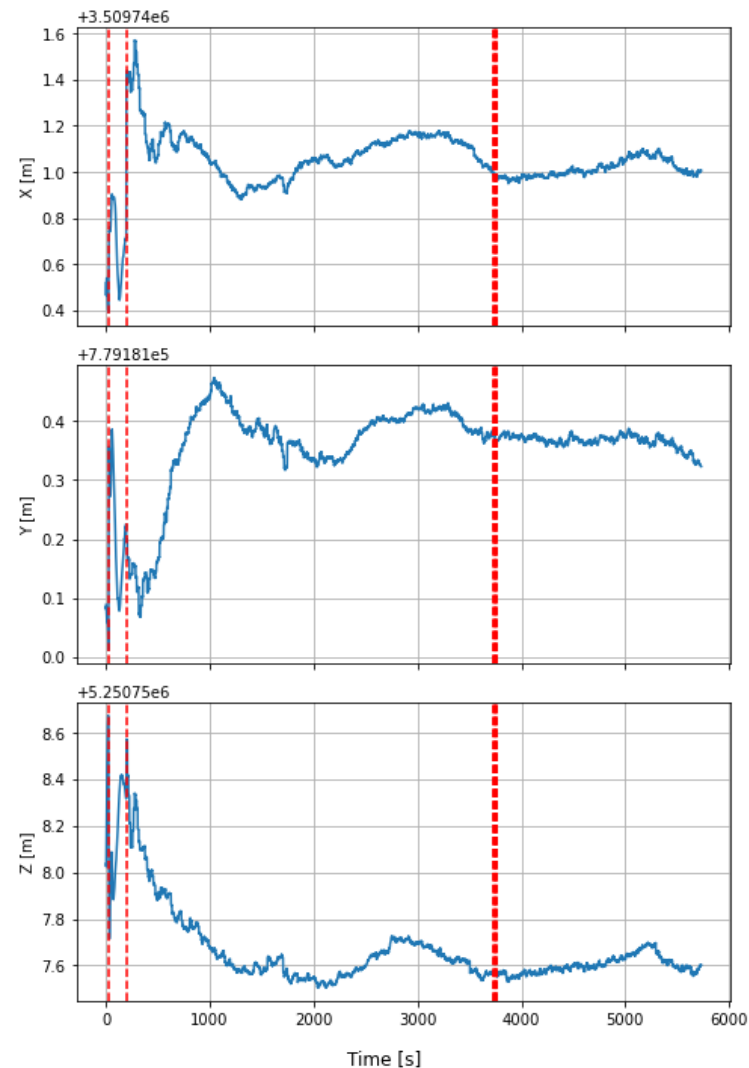
GALHAS FLT achieved after: 4.43 minutes

# Semi-urban conditions

- Location C (Open field with few trees and tall buildings nearby).
- Connected Arrow to the EOS antenna placed on a tripod.
- Partial view of the sky from a ground location.
- 1 test was carried out.
- Testing possibility of Galileo HAS Float/Fixed on ground location with more ideal conditions.



# Semi-urban conditions



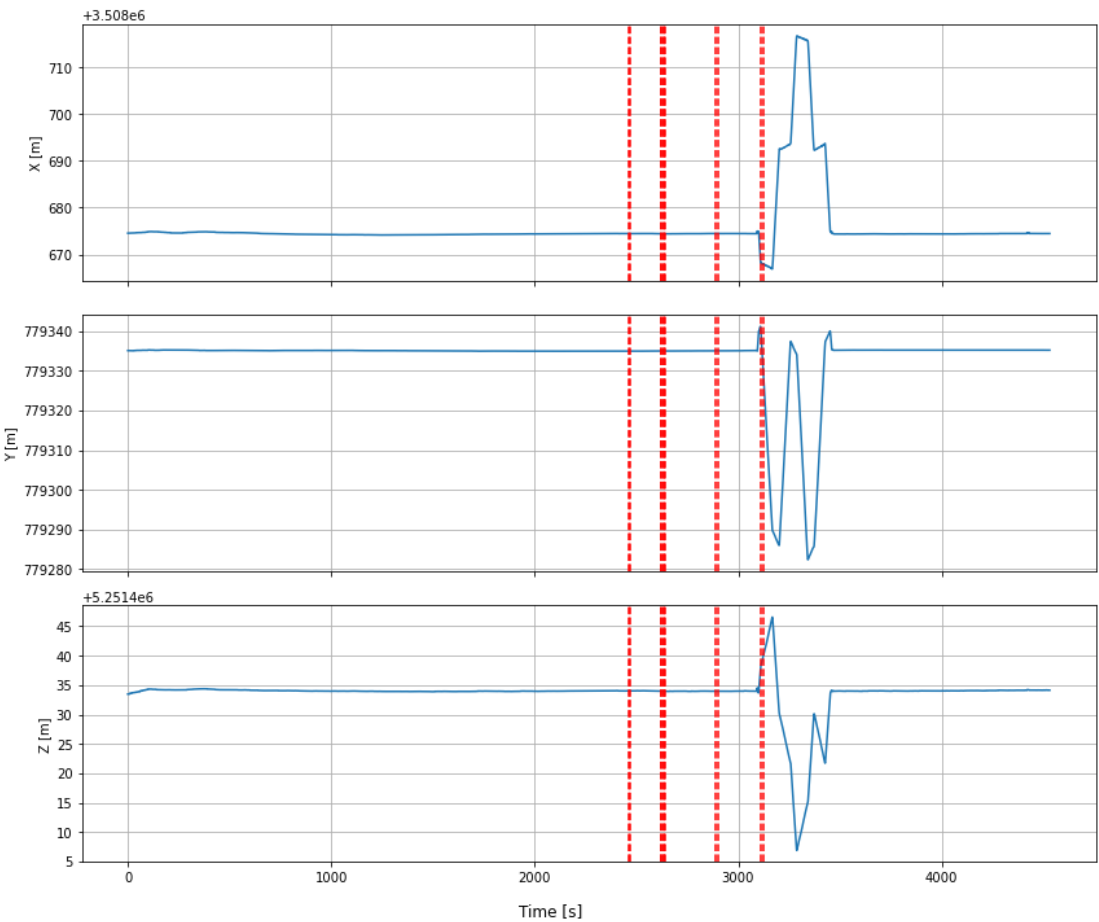
GALHAS FIX achieved after: 62.77 minutes

# Kinematic test

- Location D (Football field with open sky conditions).
- Connected Arrow to the EOS antenna placed on a tripod.
- Good sky view from the ground.
- 2 tests were carried out.
- Testing possibility of Galileo HAS Float/Fixed on the ground and the signal quality while performing a kinematic test.

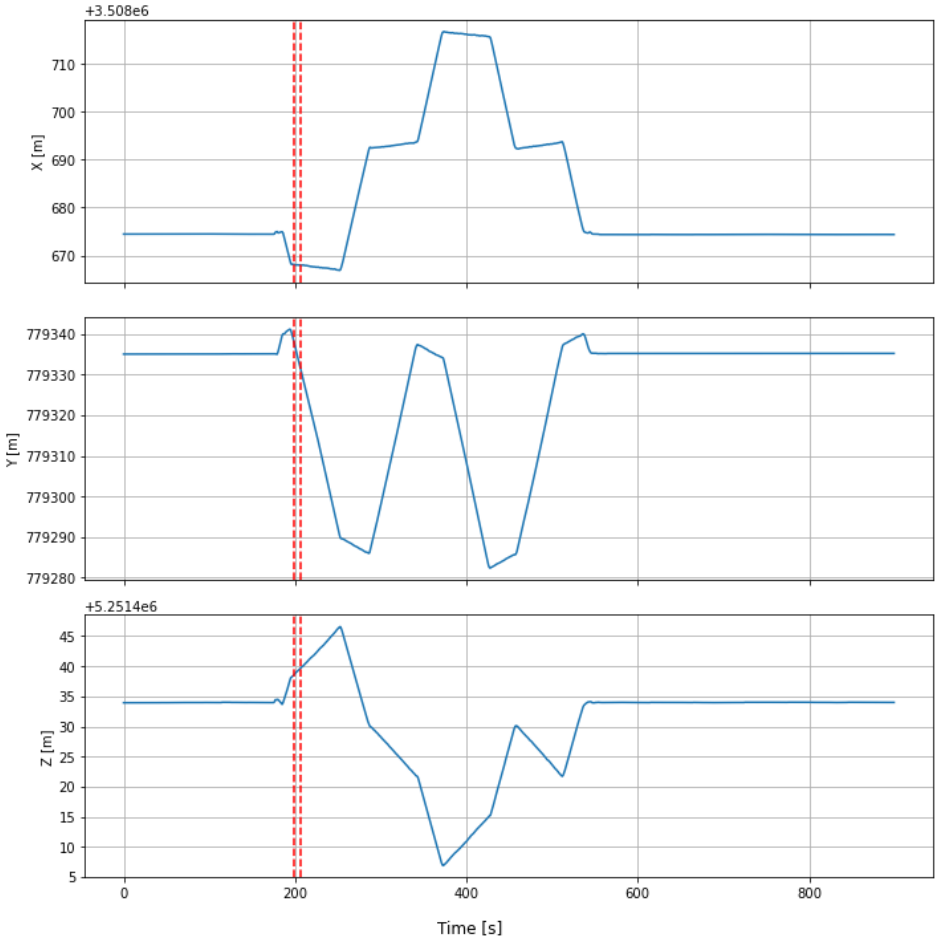


# Kinematic test 1



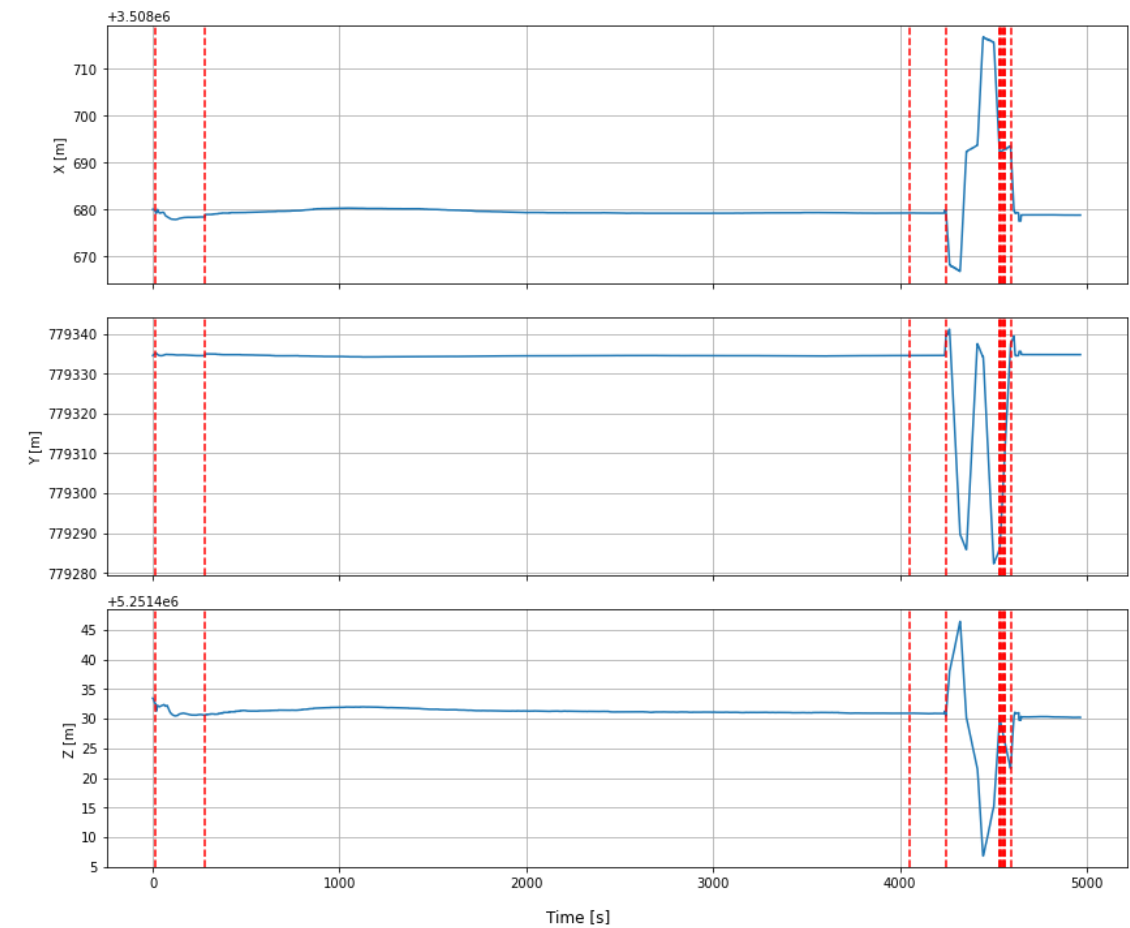
GALHAS FIX achieved after: 41.0 minutes

(Zoom-in of the walking segment only)

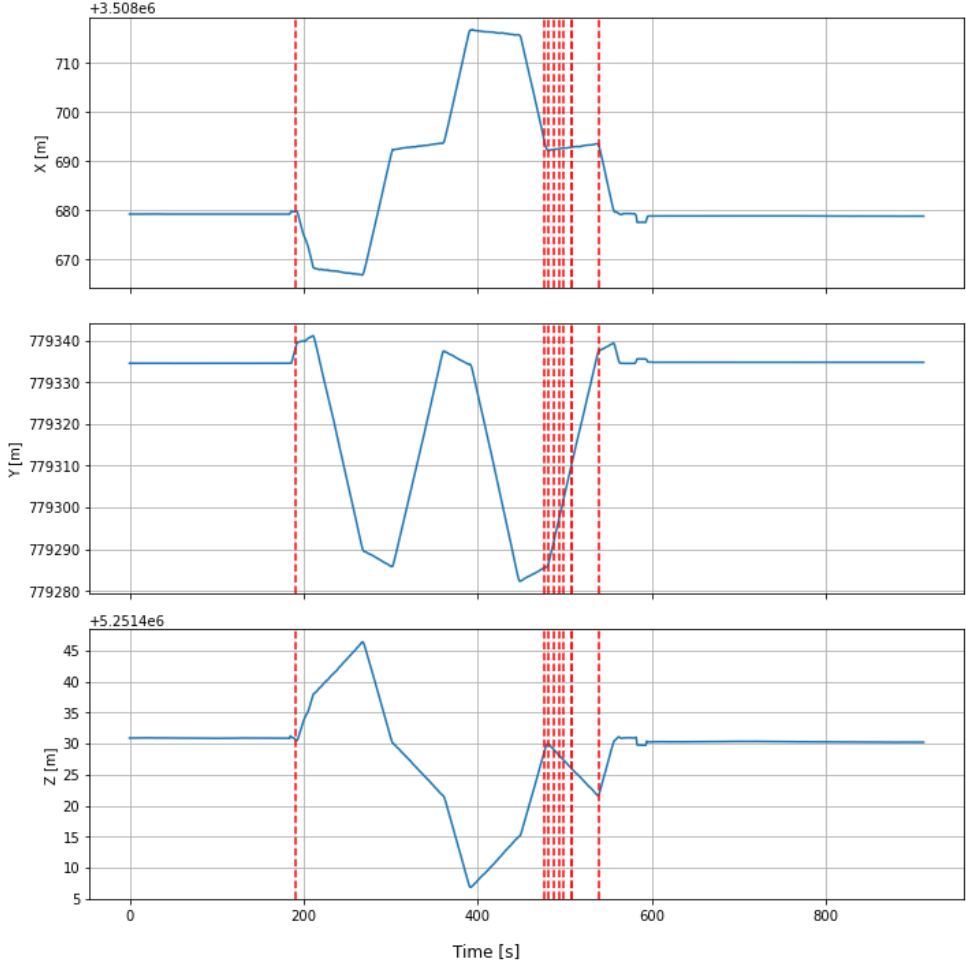


# Kinematic test 2

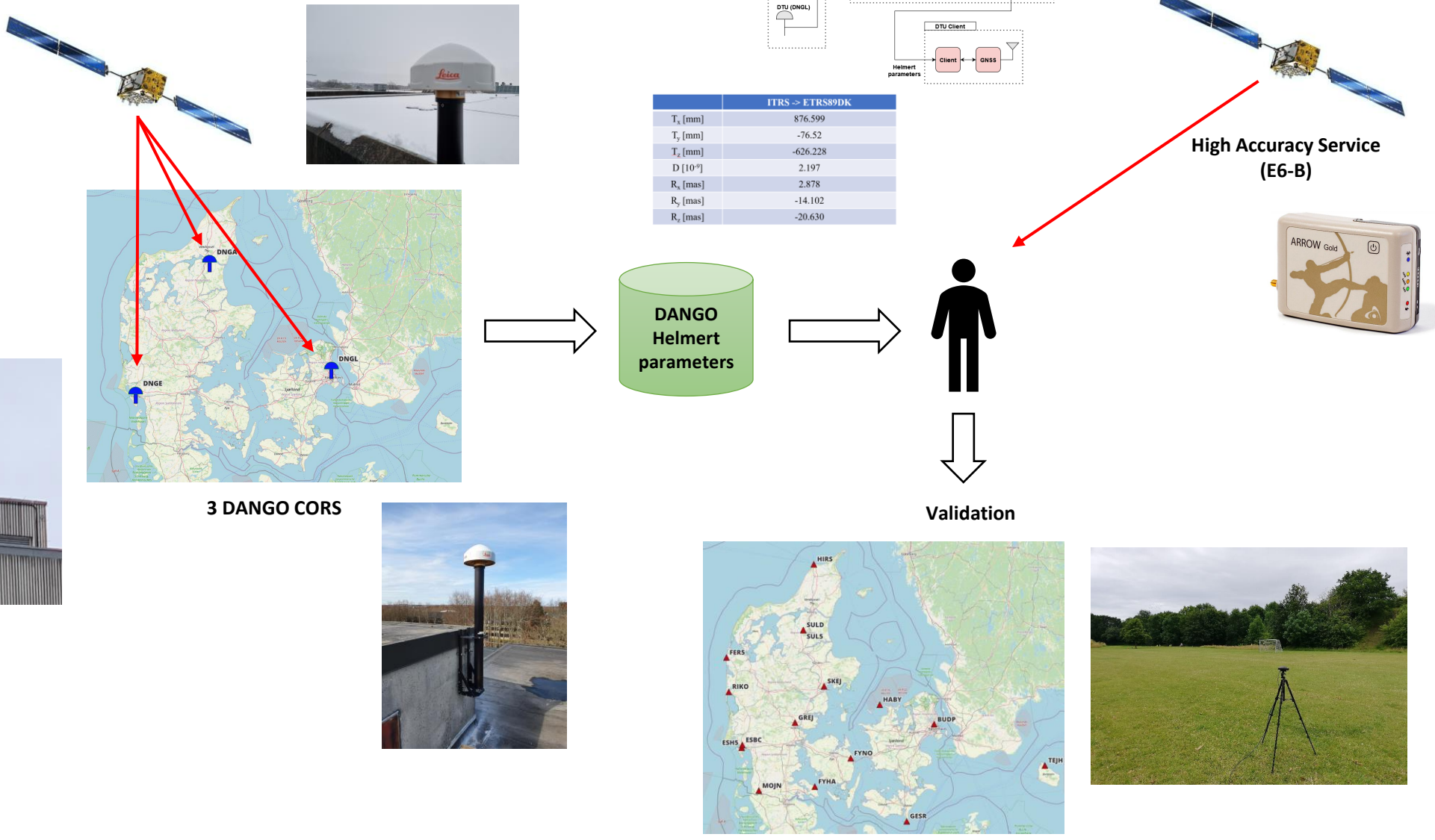
(Zoom-in of the walking segment only)



GALHAS FIX achieved after: 67.57 minutes



# Conclusion



3 DANGO CORS

Validation

High Accuracy Service (E6-B)

# DTU

